CS 525: Advanced Database Organization
06: Even more index structures

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Slides: adapted from a course taught by Hector Garcia-Molina, Stanford InfoLab

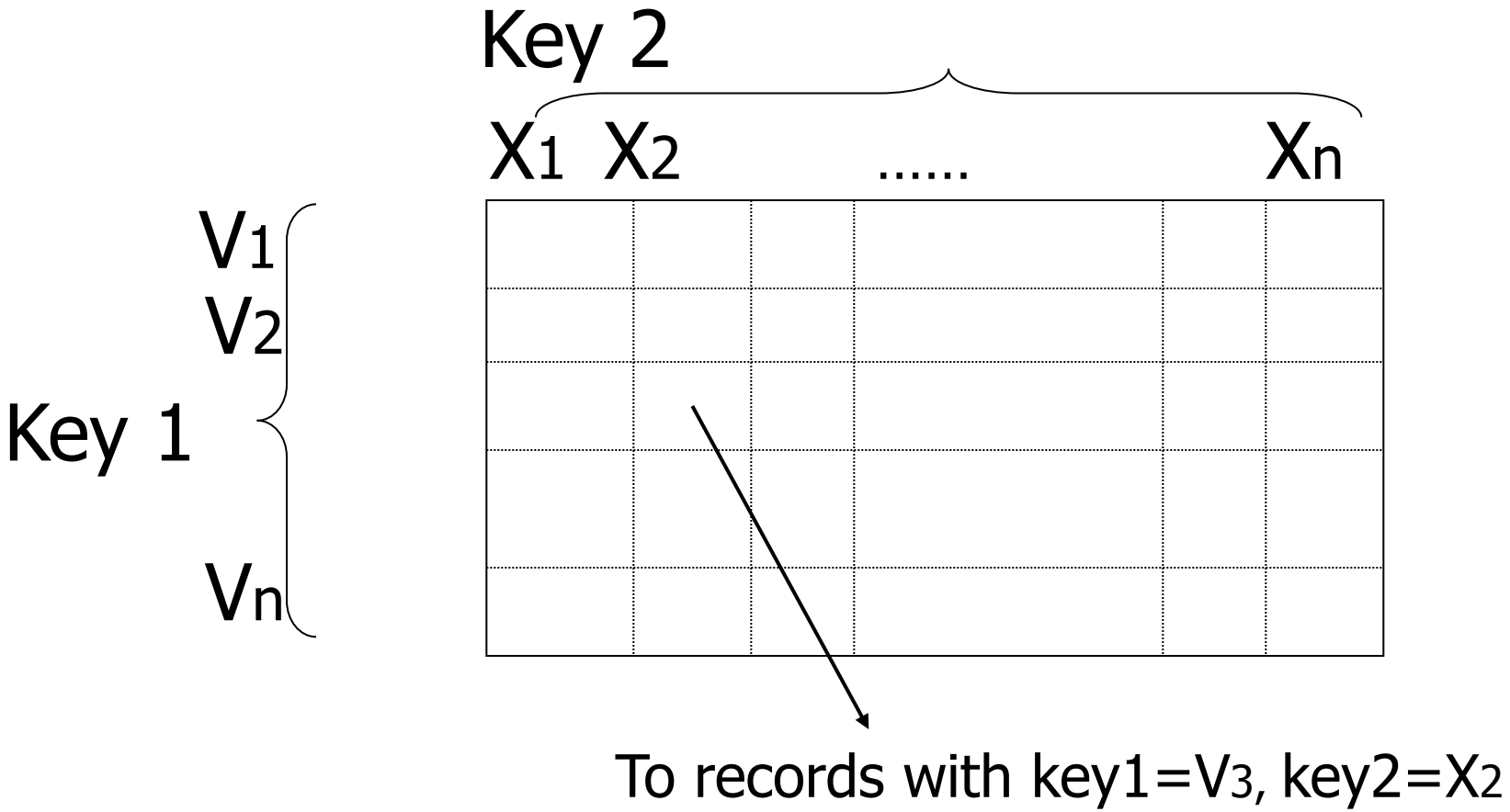
Recap

- We have discussed
  - Conventional Indices
  - B-trees
  - Hashing
  - Trade-offs
  - Multi-key indices
  - Multi-dimensional indices
    - … but no example

Today

- **Multi-dimensional index structures**
  - kd-Trees (very similar to example before)
  - **Grid File (Grid Index)**
  - Quad Trees
  - **R Trees**
  - **Partitioned Hash**
  - …
- **Bitmap-indices**
- **Tries**

Grid Index



CLAIM

- Can quickly find records with
  - key 1 = V_i $\wedge$ Key 2 = X_j
  - key 1 = V_i
  - key 2 = X_j

CLAIM

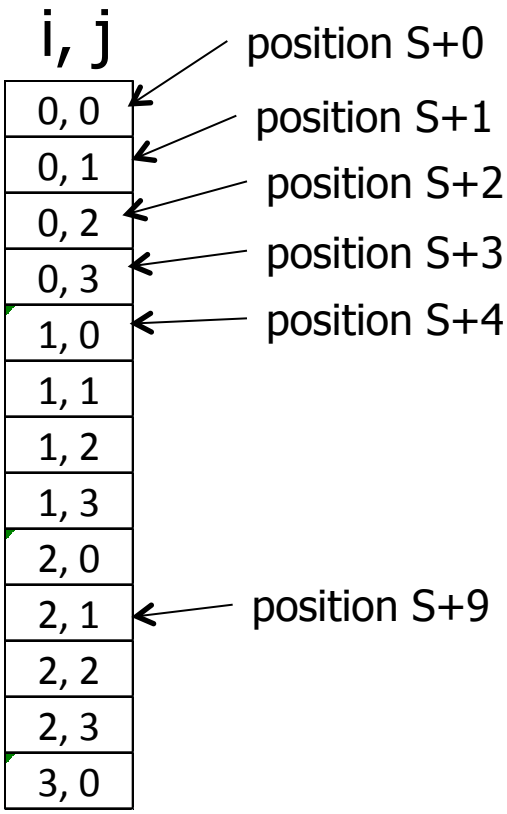
- Can quickly find records with
  - key 1 = V_i ∧ Key 2 = X_j
  - key 1 = V_i
  - key 2 = X_j

- And also ranges….
  - E.g., key 1 ≥ V_i ∧ key 2 < X_j

- How do we find entry i,j in linear structure?

max number of
i values N=4

pos(i, j) =



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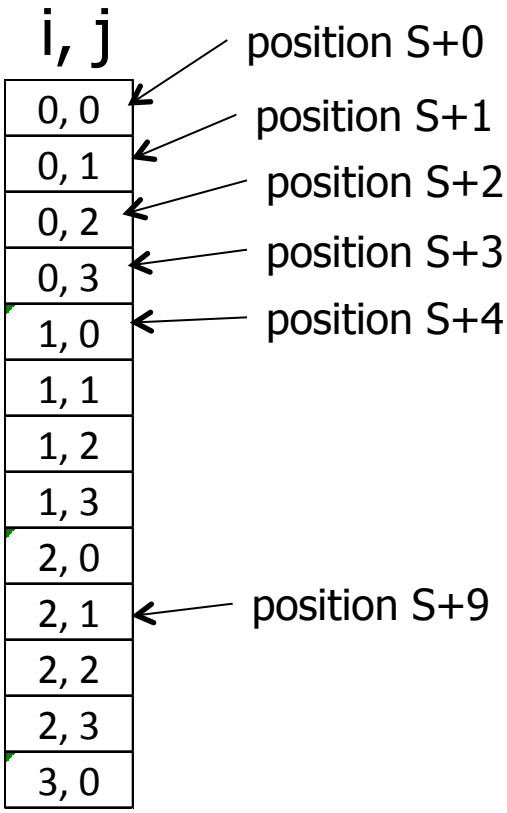
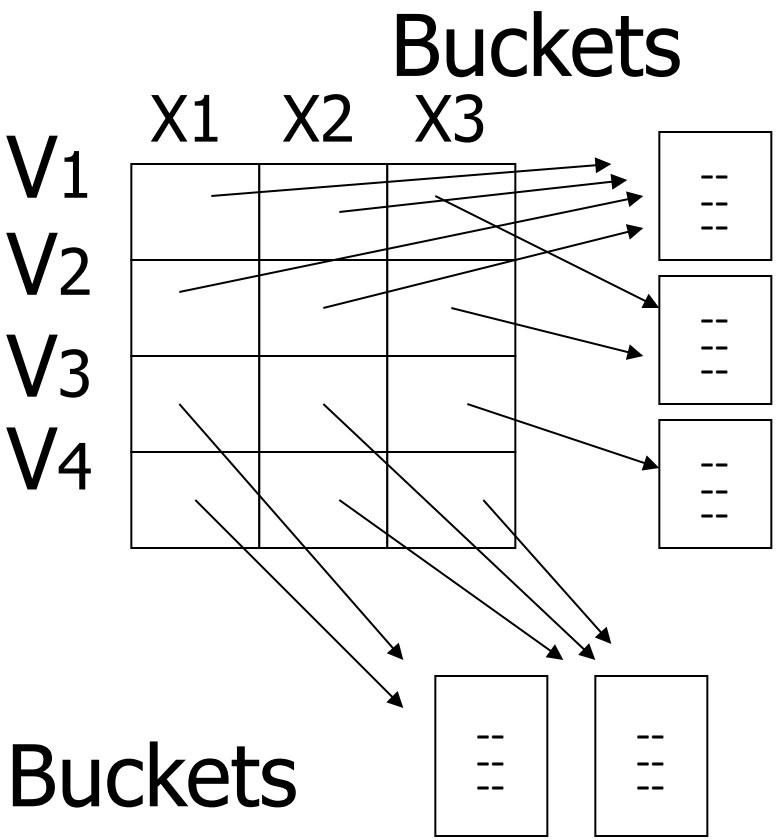


$$pos(i, j) = S + iN + j$$

Issue: Cells must be same size, and N must be constant!

Issue: Some cells may overflow, some may be sparse...

Solution: Use Indirection



*Grid only contains pointers to buckets

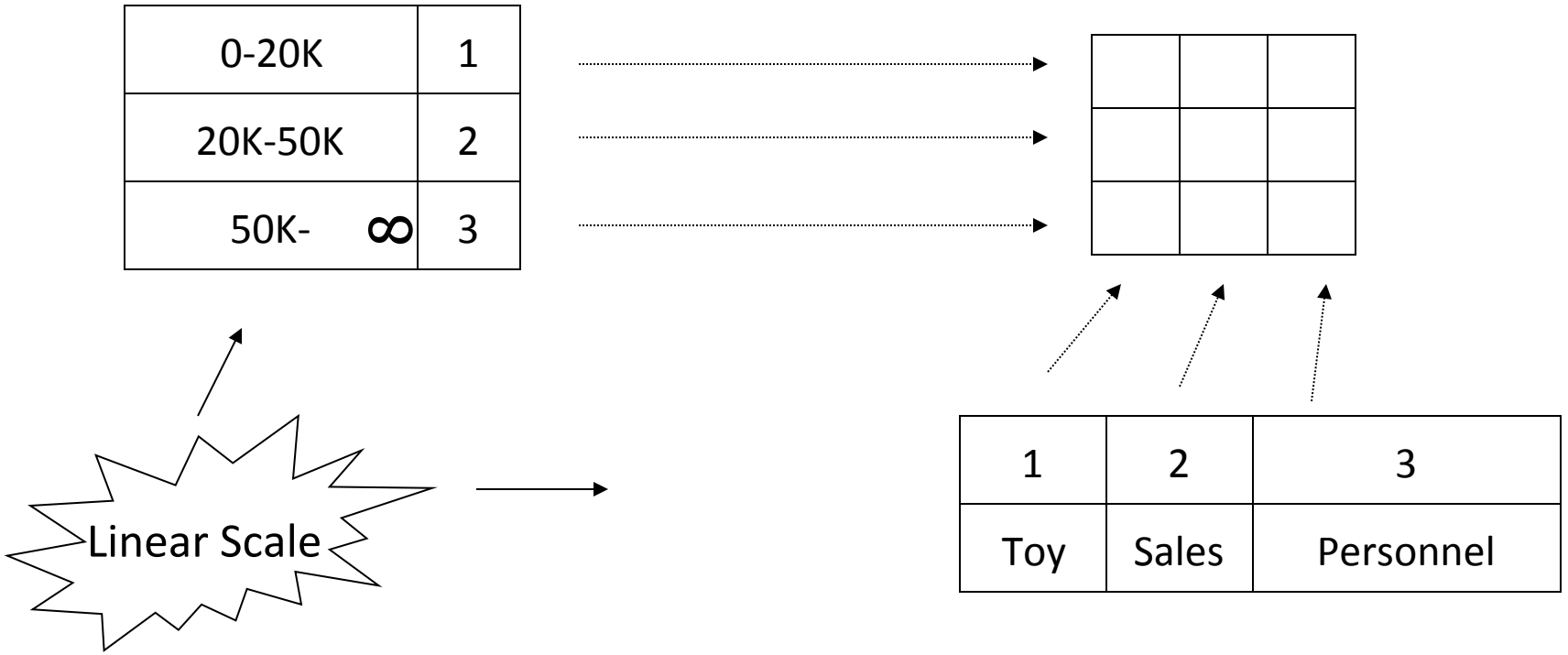
With indirection:

- Grid can be regular without wasting space
- We do have price of indirection

Can also index grid on value ranges

Salary

Grid



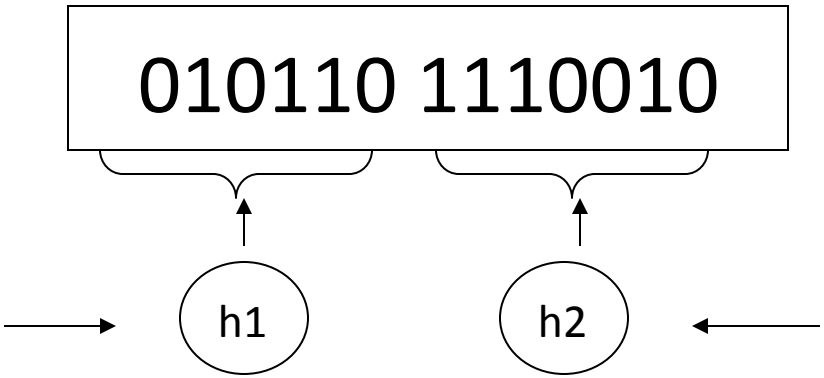
Grid files

- ⊕ Good for multiple-key search
- ⊖ Space, management overhead

  (nothing is free)
- ⊖ Need partitioning ranges that evenly split keys

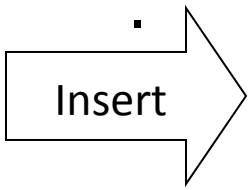
Partitioned hash function

Idea:

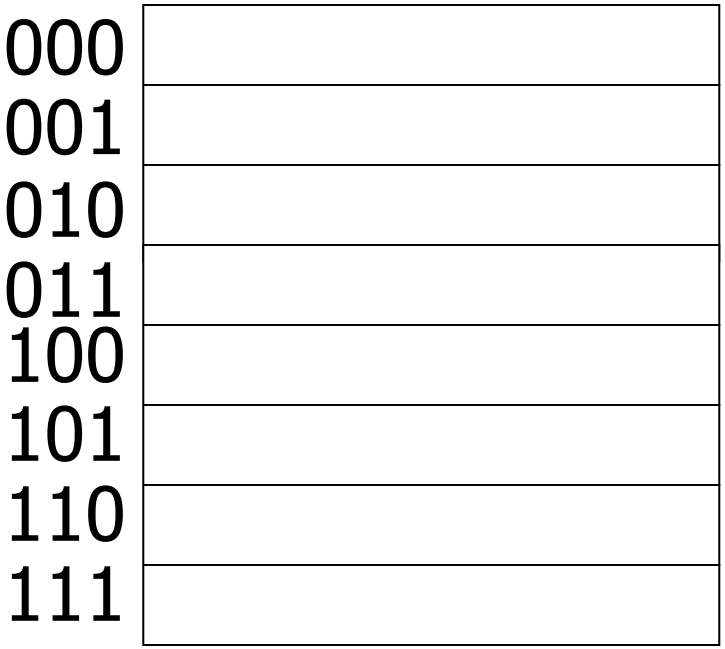


EX:

h1(toy) =0
h1(sales) =1
h1(art) =1
.
h2(10k) =01
h2(20k) =11
h2(30k) =01
h2(40k) =00
.



<Fred,toy,10k>,<Joe,sales,10k>
<Sally,art,30k>



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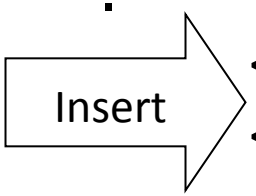

<Fred,toy,10k>,<Joe,sales,10k>
<Sally,art,30k>

000	
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010	
011	
100	
101	<Joe><Sally>
110	
111	

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011	
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101	
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111	<Andy>

Find Emp. with Dept. = Sales ∧ Sal=40k

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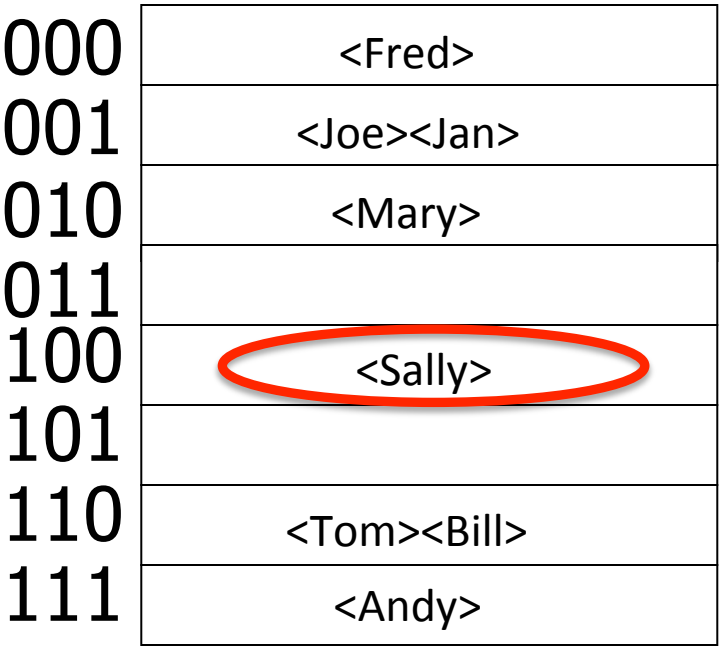

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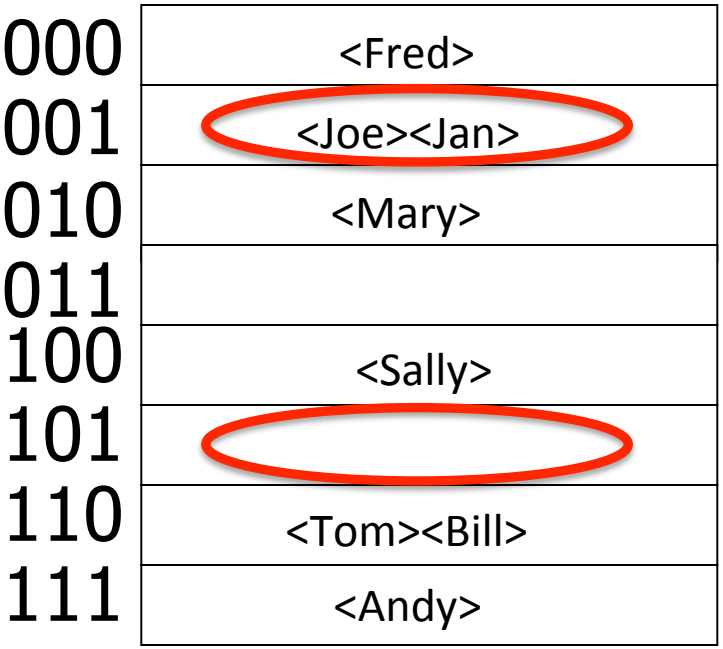

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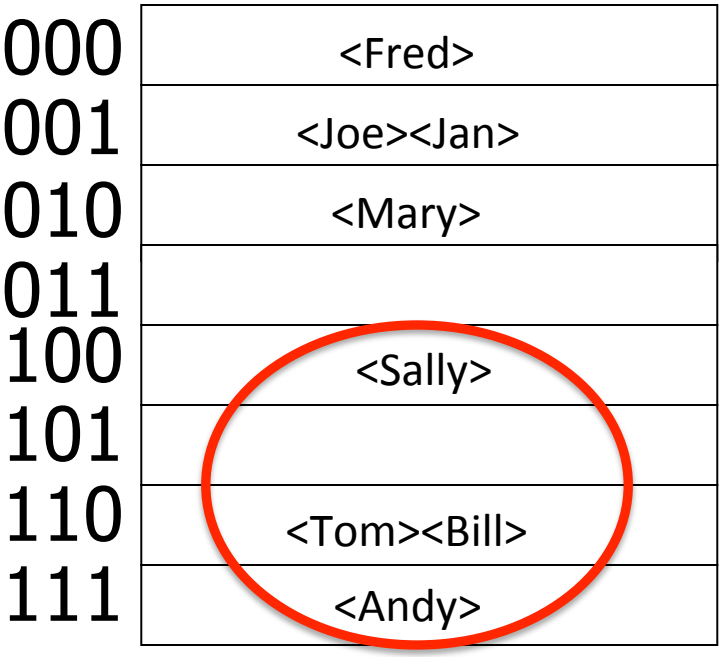
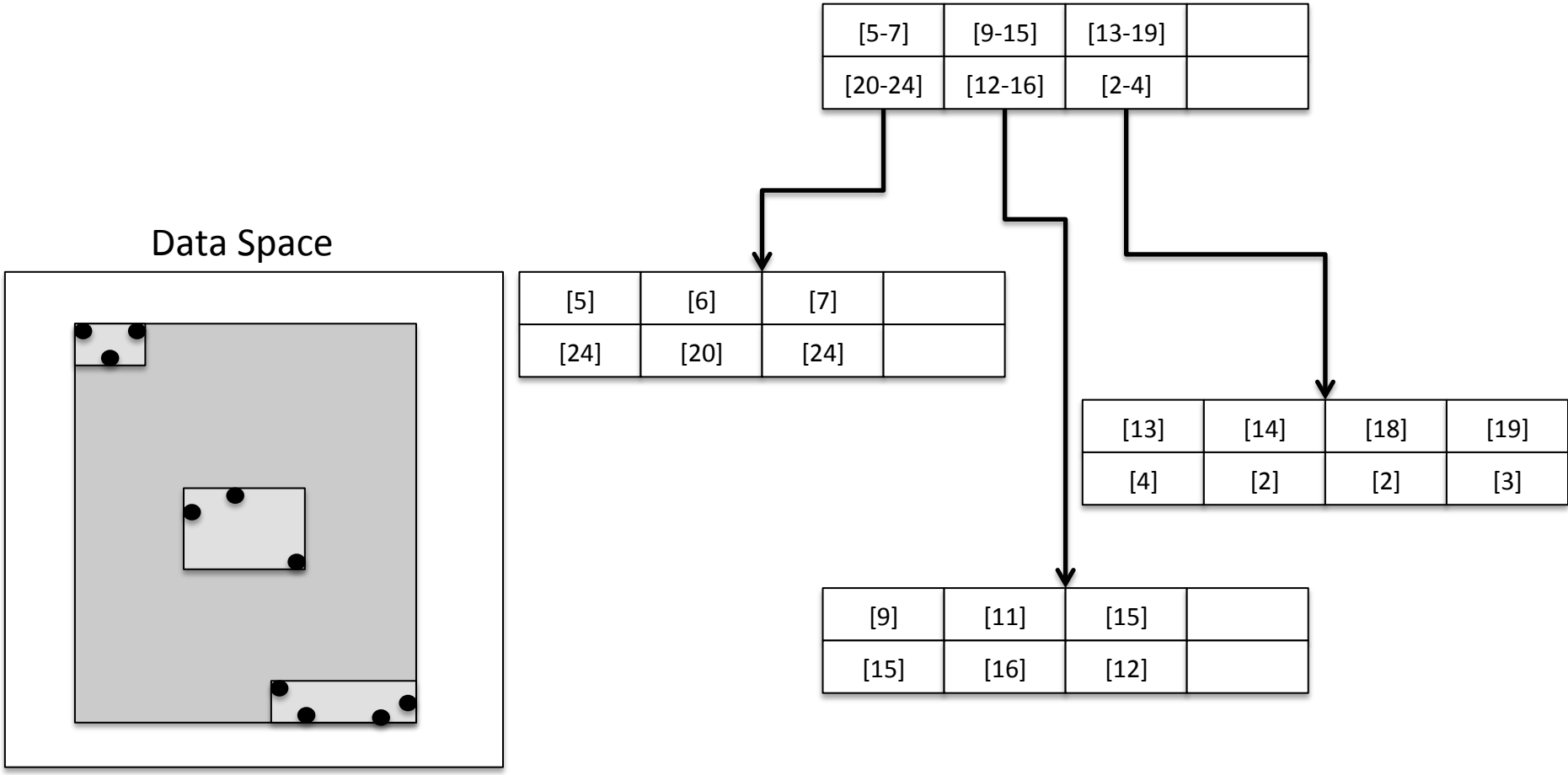


Find Emp. with Dept. = Sales

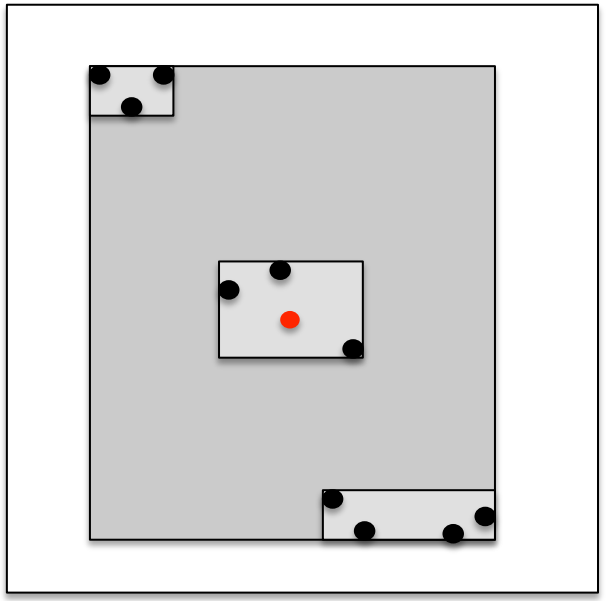
R-tree

- Nodes can store up to **M** entries
  - Minimum fill requirement (depends on variant)
- Each node rectangle in **n**-dimensional space
  - Minimum Bounding Rectangle (MBR) of its children
- MBRs of siblings are allowed to overlap
  - Different from B-trees
- balanced


Data Space
[5-7]
[9-15]
[13-19]
[20-24]
[12-16]
[2-4]
[5]
[6]
[7]
[24]
[20]
[24]
[13]
[14]
[18]
[19]
[4]
[2]
[2]
[3]
[9]
[11]
[15]
[15]
[16]
[12]

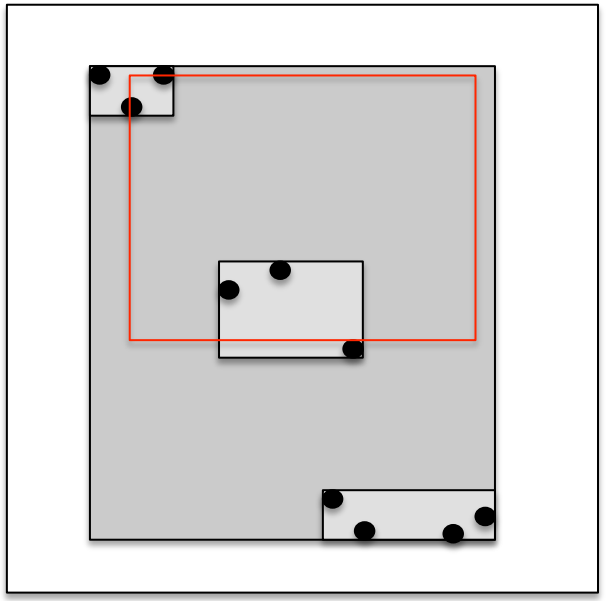
R-tree - Search

- Point Search
  - Search for p = <x_i, y_i>
  - Keep list of potential nodes
    - Needed because of overlap
  - Traverse to child if MBR of child contains p

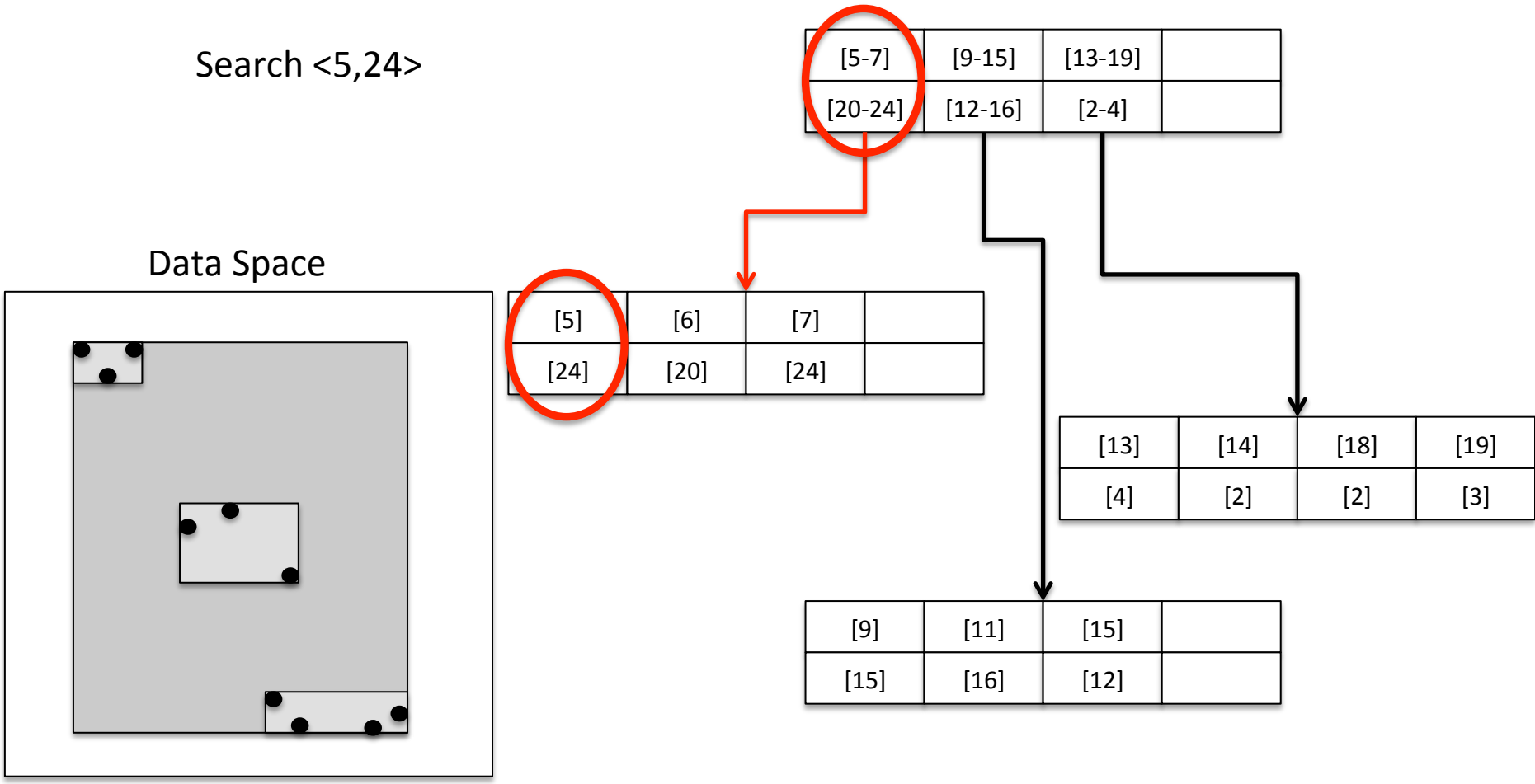


R-tree - Search

- Point Search
  - Search for points in region = <[x_{min}- x_{max}], [y_{min} -y_{max}]>
  - Keep list of potential nodes
  - Traverse to child if MBR of child overlaps with query region



Search <5,24>


[5-7]
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[2-4]
[5]
[6]
[7]
[24]
[20]
[24]
[13]
[14]
[18]
[19]
[4]
[2]
[2]
[3]
[9]
[11]
[15]
[15]
[16]
[12]
Data Space

R-tree - Insert

- Similar to B-tree, but more complex
  - Overlap -> multiple choices where to add entry
  - Split harder because more choice how to split node (compare B-tree = 1 choice)
- 1) Find potential subtrees for current node
  - Choose one for insert (heuristic, e.g., the one the would grow the least)
  - Continue until leaf is found

R-tree - Insert

- 2) Insert into leaf
- 3) Leaf is full? -> split
  - Find best split (minimum overlap between new nodes) is hard ($O(2^M)$)
  - Use linear or quadratic heuristics (original paper)
- 4) Adapt parents if necessary

R-tree - Delete

- 1) Find leaf node that contains entry
- 2) Delete entry
- 3) Leaf node underflow?
  - Remove leaf node and cache entries
  - Adapt parents
  - Reinsert deleted entries

Bitmap Index

- Domain of values D = $\{d_1, \ldots, d_n\}$
  - Gender {male, female}
  - Age {1, …, 120?}
- Use one vector of bits for each value
  - One bit for each record
    - 0: record has different value in this attribute
    - 1: record has this value

Bitmap Index Example

Age

1	2	3
1	0	0
0	1	0
1	0	0
0	0	1

Todlers

Name	Age	Gender
Peter	1	male
Gertrud	2	female
Joe	1	male
Marry	3	female

Gender

male	female
1	0
0	1
1	0
0	1

Bitmap Index Example

Age

1	2	3
1	0	0
0	1	0
1	0	0
0	0	1

Todlers

Name	Age	Gender
Peter	1	male
Gertrud	2	female
Joe	1	male
Marry	3	female

Gender

male	female
1	0
0	1
1	0
0	1

Find all todlers with age **2 and** sex **female**:
Bitwise-and between vectors

■
0
1
0
0

Bitmap Index Example

Age

1	2	3
1	0	0
0	1	0
1	0	0
0	0	1

Todlers

Name	Age	Gender
Peter	1	male
Gertrud	2	female
Joe	1	male
Marry	3	female

Gender

male	female
1	0
0	1
1	0
0	1

Find all todlers with age **2 or** sex **female**:
Bitwise-or between vectors

0
1
0
1

Compression

- Observation:
  - Each record has one value in indexed attribute
  - For N records and domain of size |D|
    - Only 1/|D| bits are 1
  - -> waste of space
- Solution
  - Compress data
  - Need to make sure that **and** and **or** is still fast

Run length encoding (RLE)

- Instead of actual 0-1 sequence encode length of 0 or 1 runs
- One bit to indicate whether 0/1 run + several bits to encode run length
- But how many bits to use to encode a run length?
  - Gamma codes or similar to have variable number of bits

RLE Example

- 0001 0000 1110 1111 **(2 bytes)**
- 3, 1,4, 3, 1,4 **(6 bytes)**
- -> if we use one byte to encode a run we have 7 bits for length = max run length is 128(127)

Elias Gamma Codes

- $X = 2^N + (x \bmod 2^N)$
  - Write N as N zeros followed by one 1
  - Write $(x \bmod 2^N)$ as N bit number
- $18 = 2^4 + 2 = 000010010$

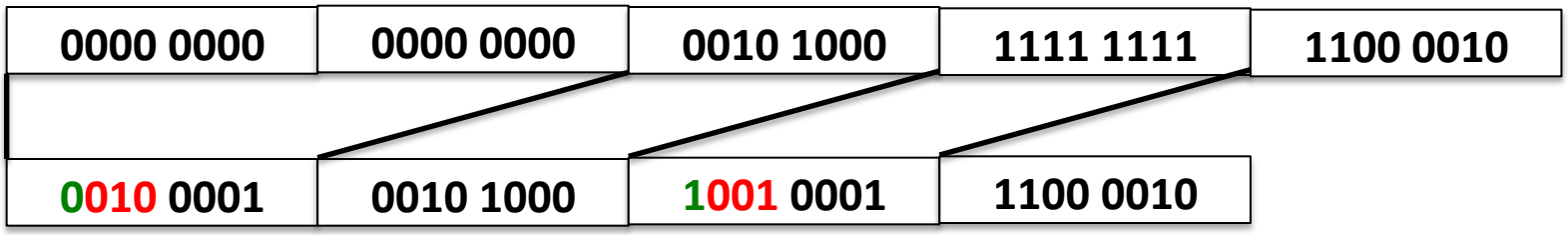
- 0001 0000 1110 1111 **(2 bytes)**
- 3, 1,4, 3, 1,4 **(6 bytes)**
- 0111 0010 0011 1001 00 **(3 bytes)**

Hybrid Encoding

- Run length encoding
  - Can waste space
  - And/or run length not aligned to byte/word boundaries
- Encode some bytes of sequence as is and only store long runs as run length
  - EWAH
  - BBC (that's what Oracle uses)

Extended Word aligned Hybrid (EWAH)

- Segment sequence in machine words (64bit)
- Use two types of words to encode
  - Literal words, taken directly from input sequence
  - Run words
    - ½ word is used to encode a run
    - ½ word is used to encode how many literals follow



Bitmap Indices

- Fast for read intensive workloads
  - Used a lot in datawarehousing
- Often build on the fly during query processing
  - As we will see later in class

Trie

- From Retrieval
- Tree index structure
- Keys are sequences of values from a domain D
  - D = {0,1}
  - D = {a,b,c,….,z}
- Key size may or may not be fixed
  - Store 4-byte integers using D = {0,1} (32 elements)
  - Strings using D={a,…,z} (arbitrary length)

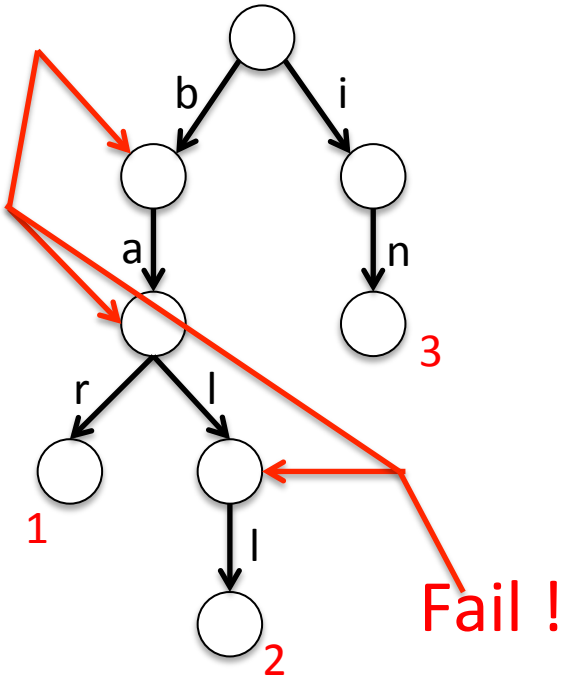
Trie

- Each node has pointers to |D| child nodes
  - One for each value of D
- Searching for a key k = $[d_1, \ldots, d_n]$
  - Start at the root
  - Follow child for value d_i

Trie Example

Words: bar, ball, in

Search for **bald**



Tries Implementation

- 1) Each node has an array of child pointers
- 2) Each node has a list or hash table of child pointers
- 3) array compression schemes derived from compressed DFA representations

Summary

Discussion:

- Conventional Indices
- B-trees
- Hashing (extensible, linear)
- SQL Index Definition
- Index vs. Hash
- Multiple Key Access
- Multi Dimensional Indices
  Variations: Grid, R-tree,
- Partitioned Hash
- Bitmap indices and compression
- Tries