CS 525: Advanced Database Organization 04: Indexing

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Slides: adapted from a <u>course</u> taught by <u>Hector Garcia-Molina</u>, Stanford InfoLab



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Part 04 Indexing & Hashing record value value ?



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Query Types:

• Point queries:

- Input: value **v** of attribute **A**
- Output: all objects (tuples) with that value in attribute A

• Range queries:

- Input: value interval [low,high] of attr A
- Output: all tuples with a value

low <= v < high in attribute A



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Index Considerations:

- Supported Query Types
- Secondary-storage capable
- Storage size
 - Index Size / Data Size
- Complexity of Operations

 E.g., insert is O(log(n)) worst-case
- Efficient Concurrent Operations?



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<u>Topics</u>

- Conventional indexes
- B-trees

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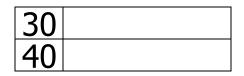
- Hashing schemes
- Advanced Index Techniques



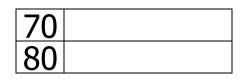


Sequential File









90	
100	

6



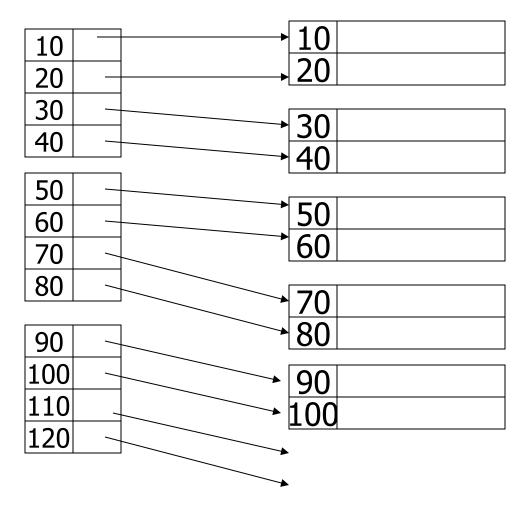
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Dense Index

Sequential File



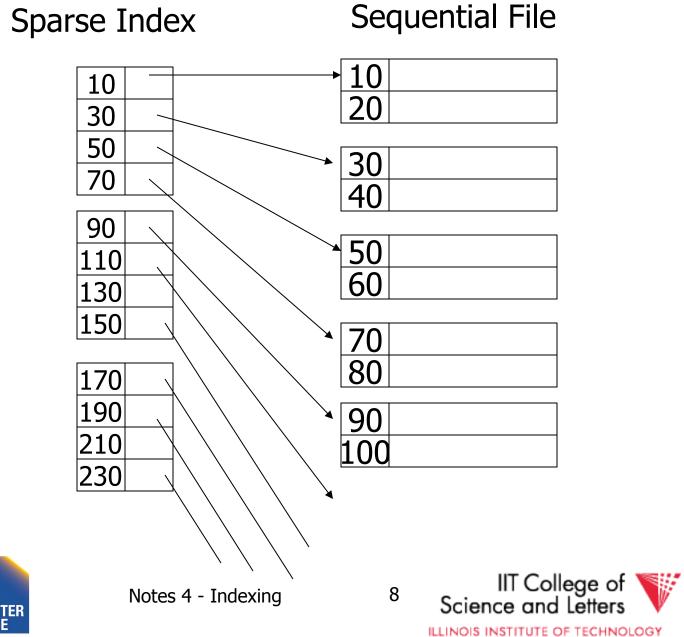
7



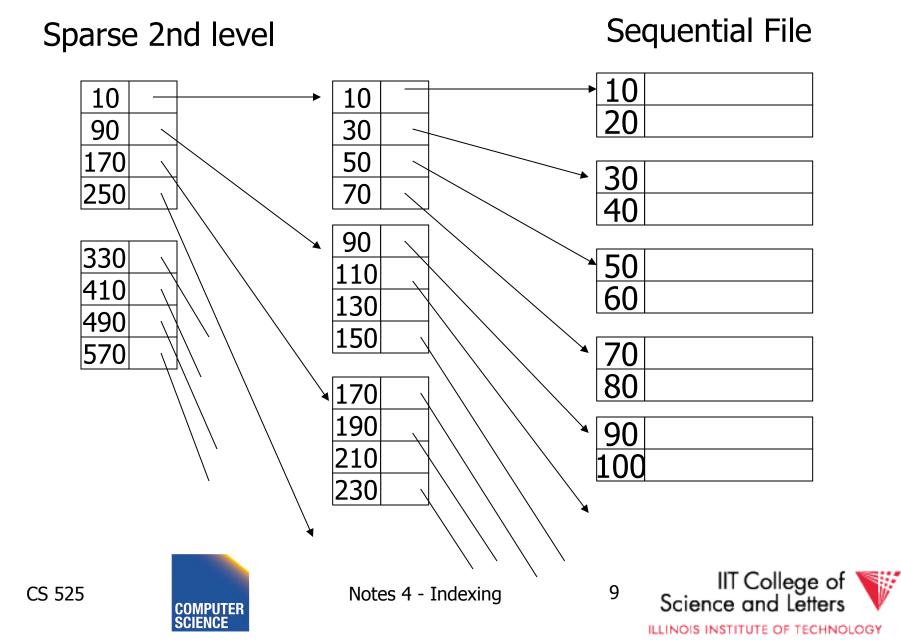
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Comment: {FILE,INDEX} may be contiguous or not (blocks chained)



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• Can we build a dense, 2nd level index for a dense index?



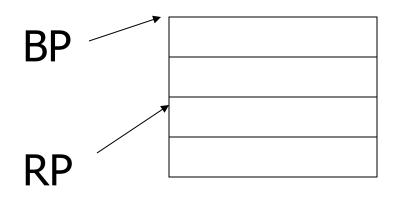
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Notes on pointers:

(1) Block pointer (sparse index) can be smaller than record pointer





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Notes on pointers:

(2) If file is contiguous, then we can omit pointers (i.e., compute them)



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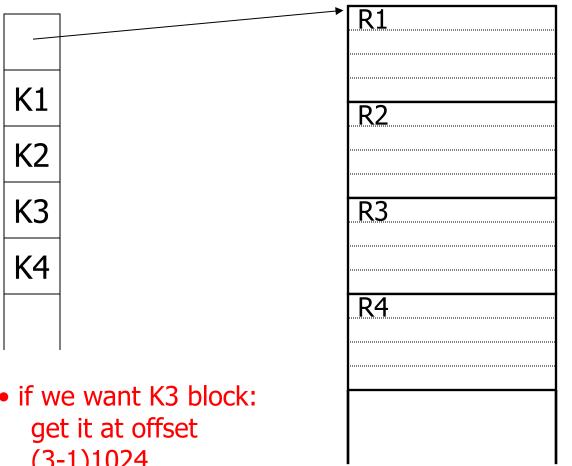
	R1	
K1	R2	
K2		
K3	R3	
K4		
	R4	
I I		



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say: 1024 B per block

• if we want K3 block: (3-1)1024 = 2048 bytes



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Sparse vs. Dense Tradeoff

• <u>Sparse:</u> Less index space per record can keep more of index

in memory

• <u>Dense:</u> Can tell if any record exists without accessing file

(Later:

- sparse better for insertions
- dense needed for secondary indexes)

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<u>Terms</u>

- Index sequential file
- Search key (≠ primary key)
- Primary index (on Sequencing field)
- Secondary index
- Dense index (all Search Key values in)
- Sparse index

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• Multi-level index





Next:

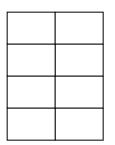
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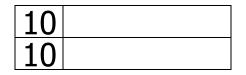
- Duplicate keys
- Deletion/Insertion
- Secondary indexes

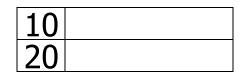


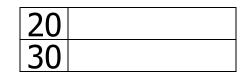
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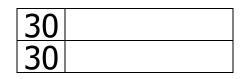












40	
45	



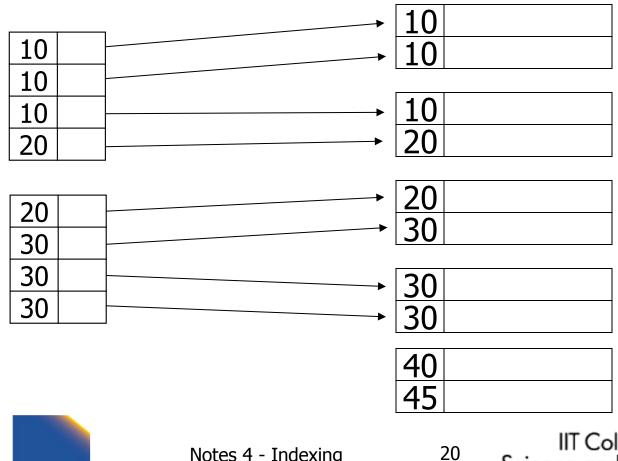
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Dense index, one way to implement?





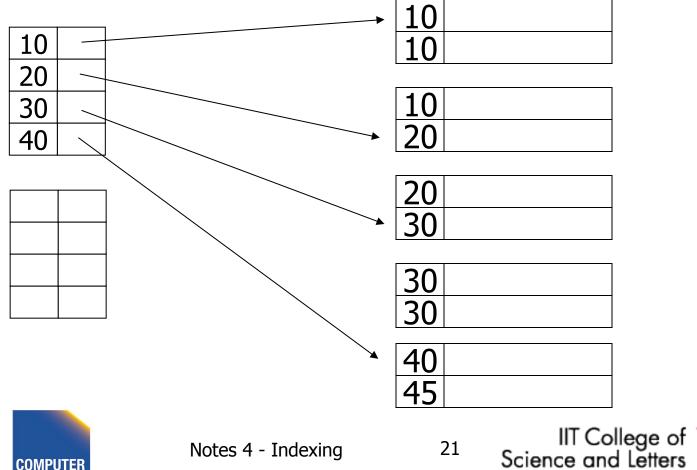
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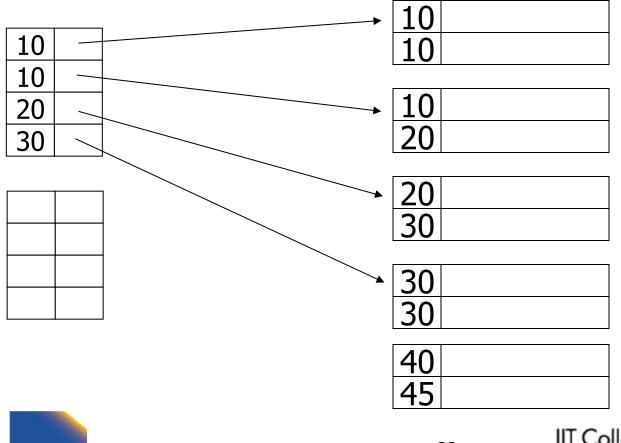
Dense index, better way?



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Sparse index, one way?





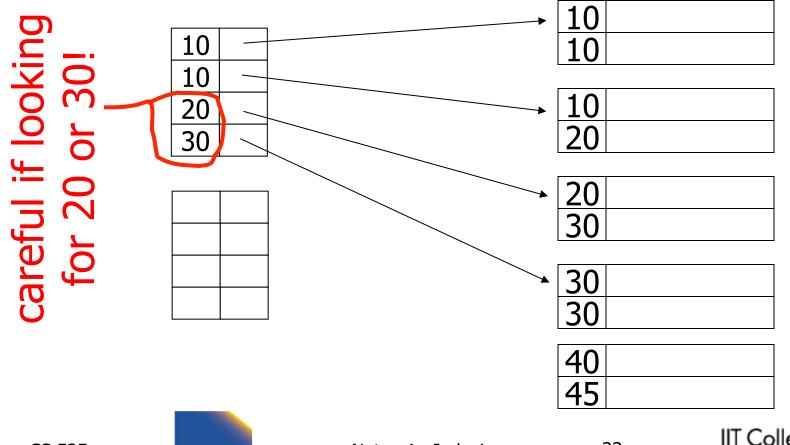
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Sparse index, one way?

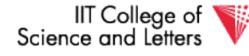




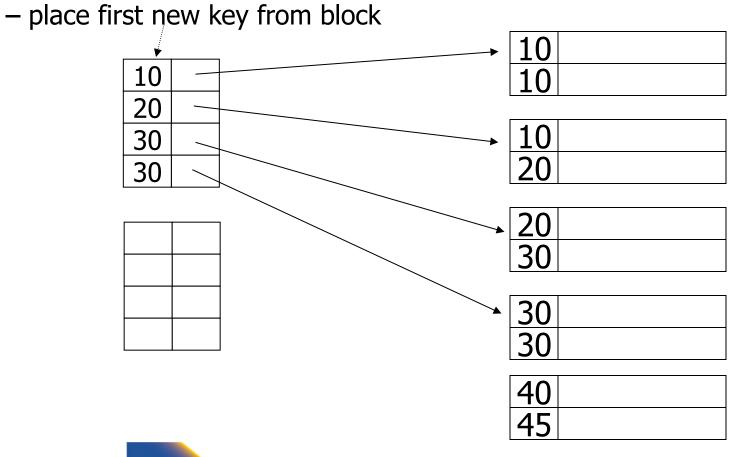


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Sparse index, another way?





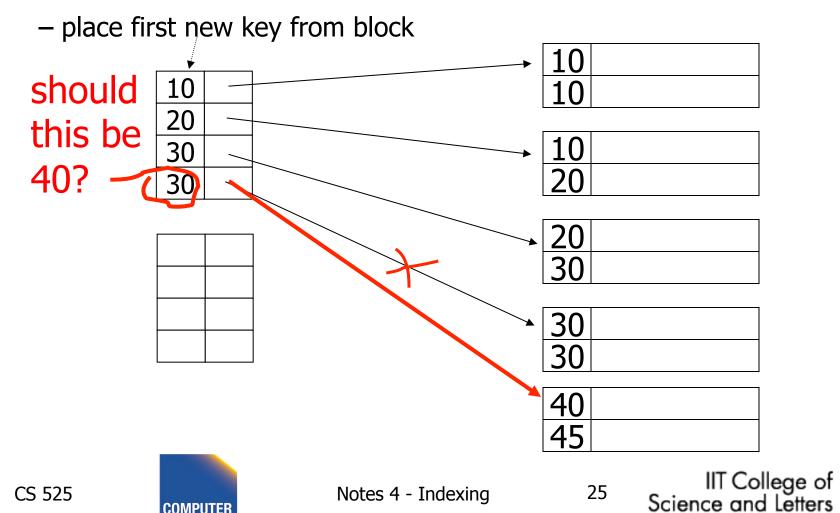
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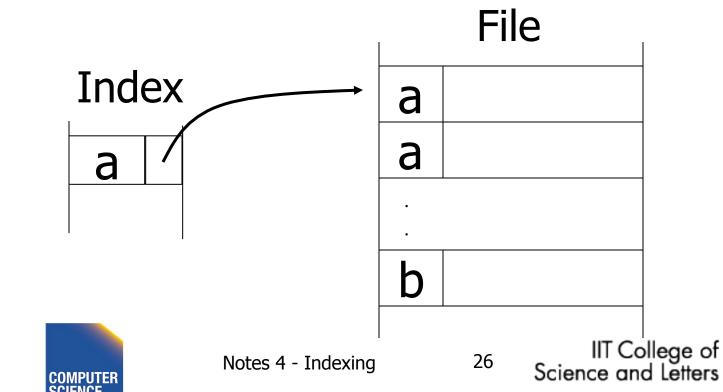


Sparse index, another way?

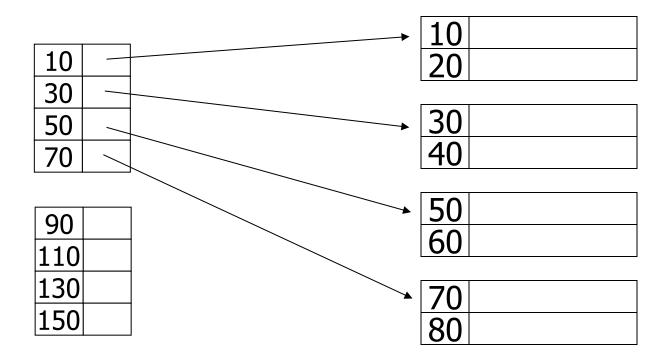


Summary Duplicate values, primary index

Index may point to <u>first</u> instance of each value only



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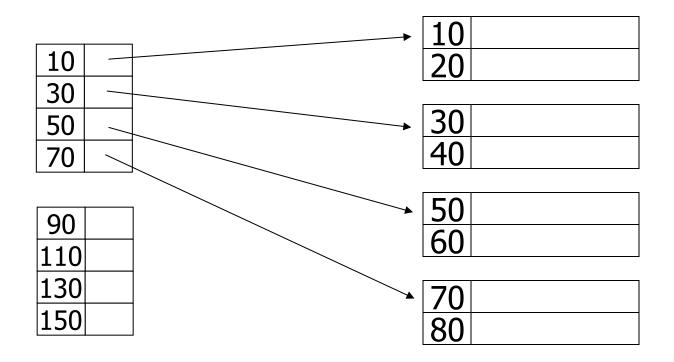
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- delete record 40



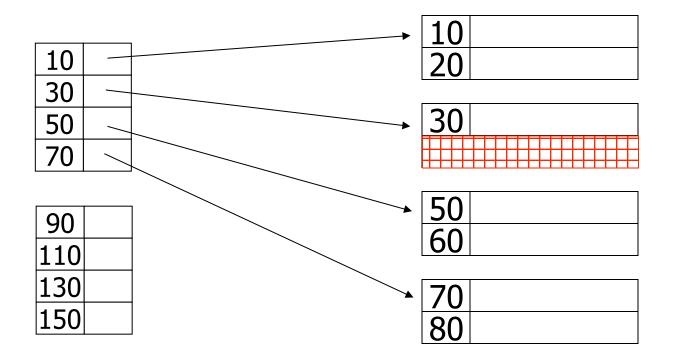


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- delete record 40



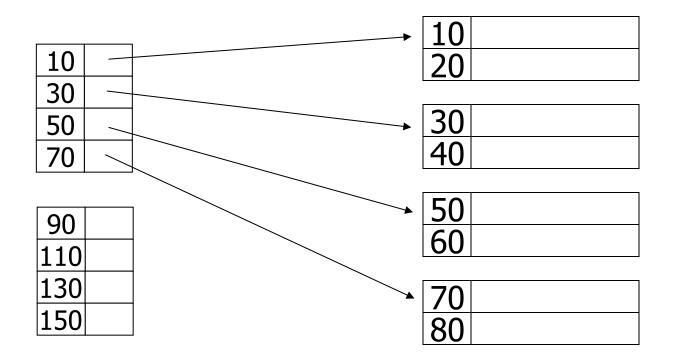


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- delete record 30

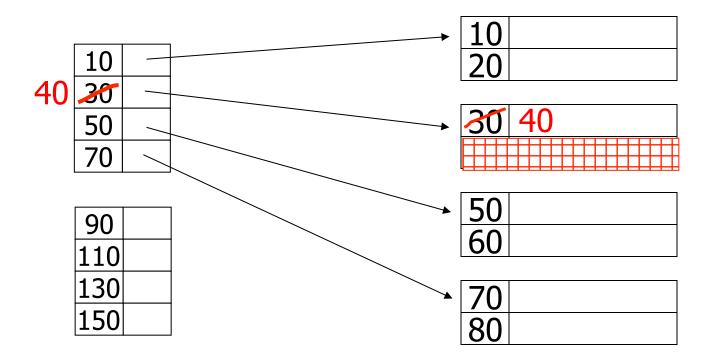




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- delete record 30



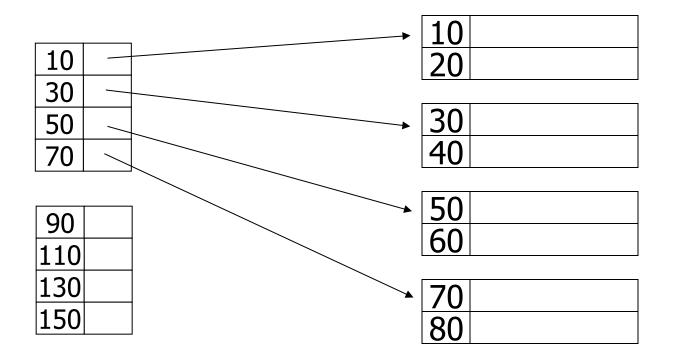


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– delete records 30 & 40



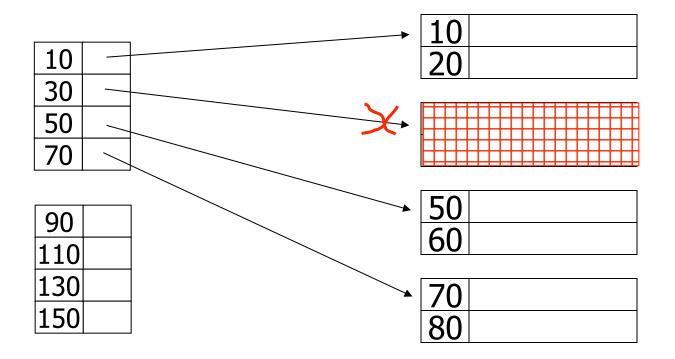


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– delete records 30 & 40



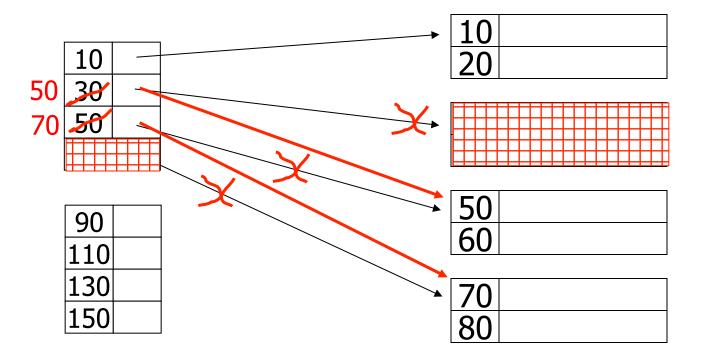


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– delete records 30 & 40



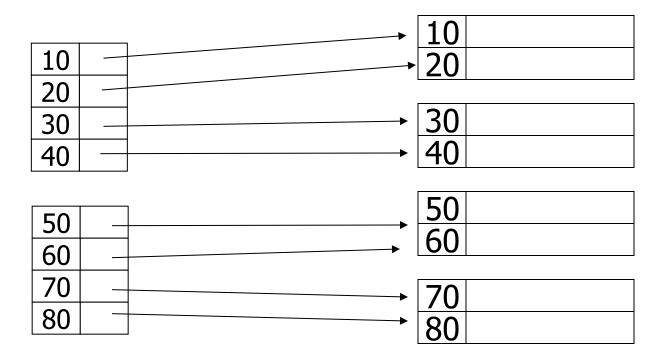


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Deletion from dense index





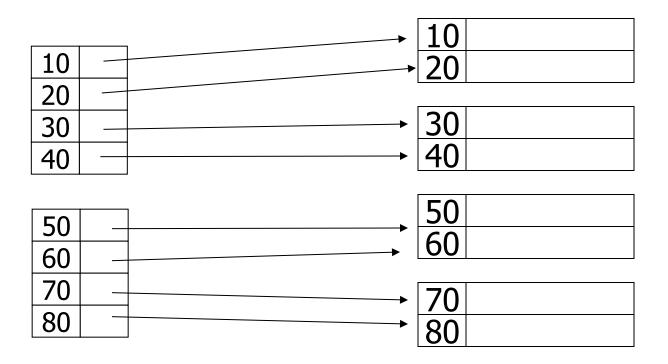
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Deletion from dense index

- delete record 30





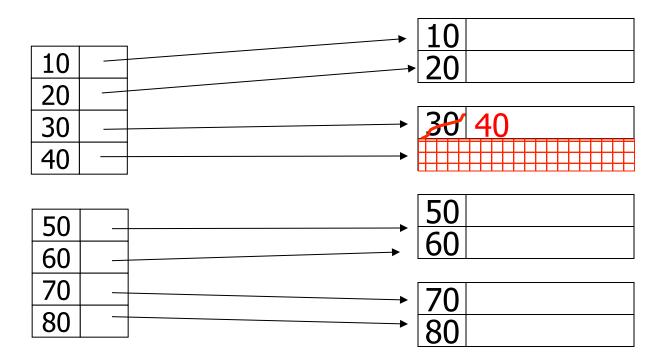
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Deletion from dense index

- delete record 30





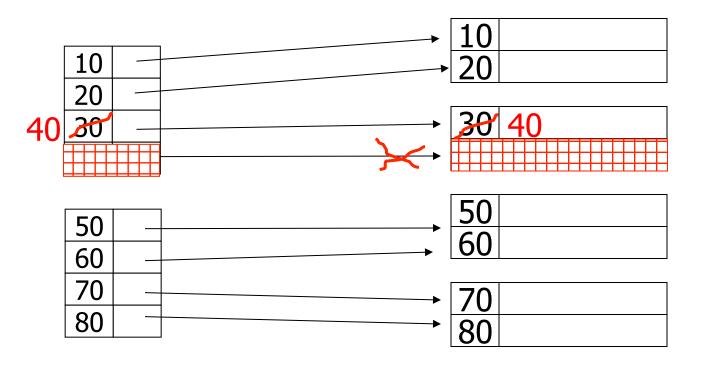
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Deletion from dense index

- delete record 30

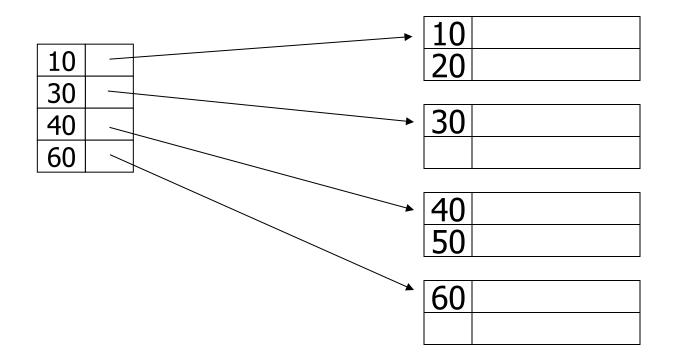




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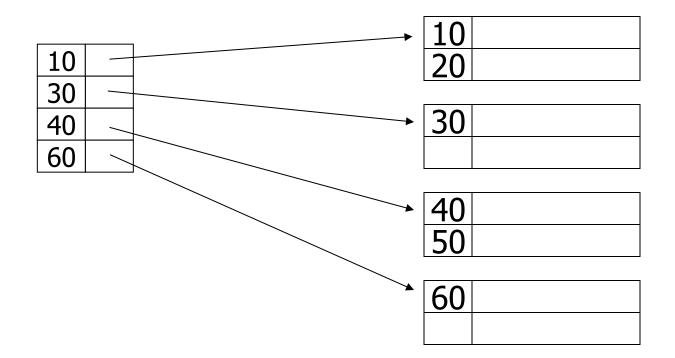
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- insert record 34



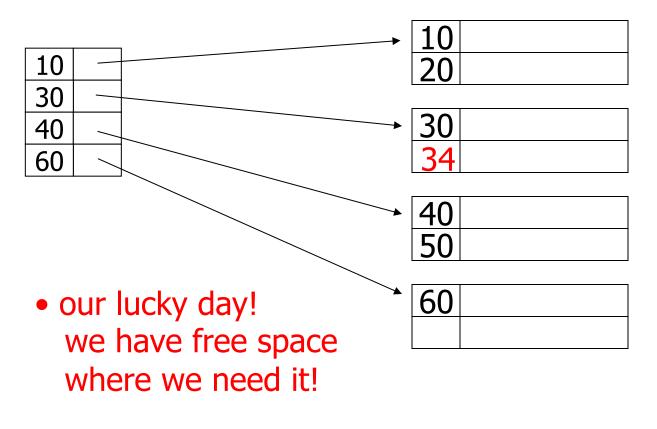


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- insert record 34





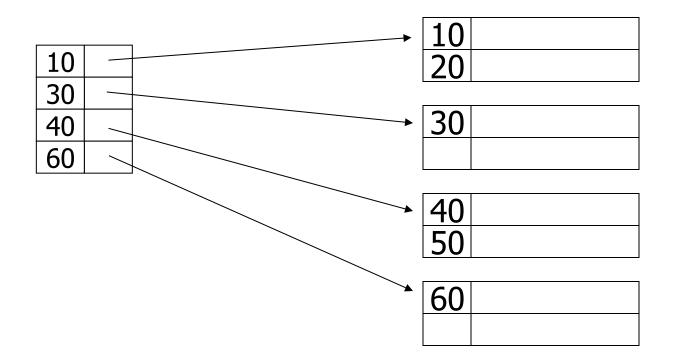
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- insert record 15



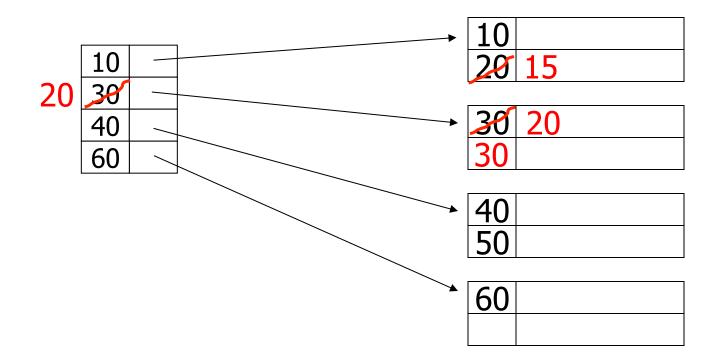


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- insert record 15



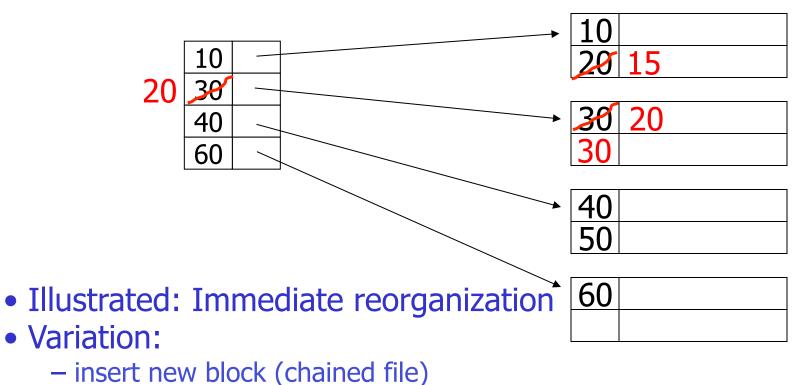


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- insert record 15



– update index

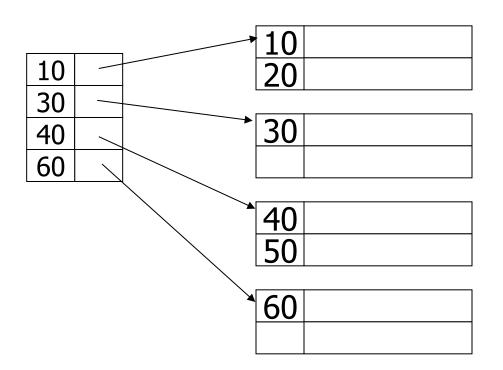
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- insert record 25

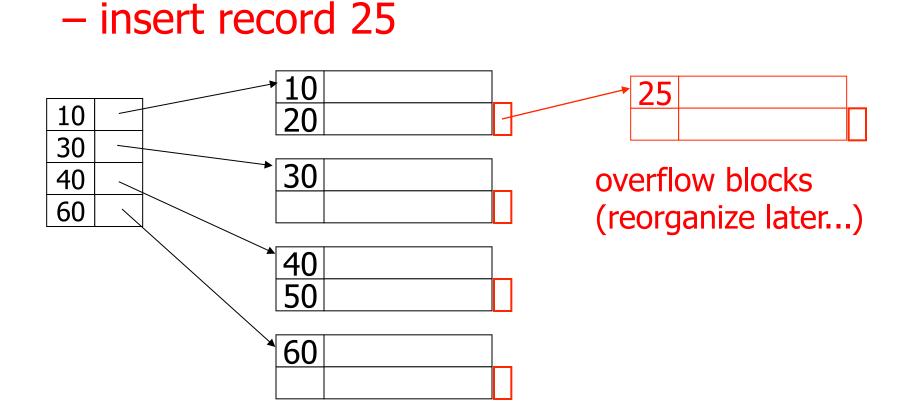




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Insertion, dense index case

- Similar
- Often more expensive . . .

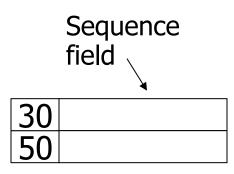


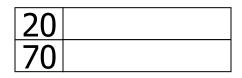
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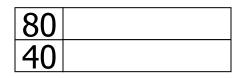
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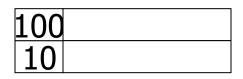


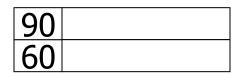
Secondary indexes













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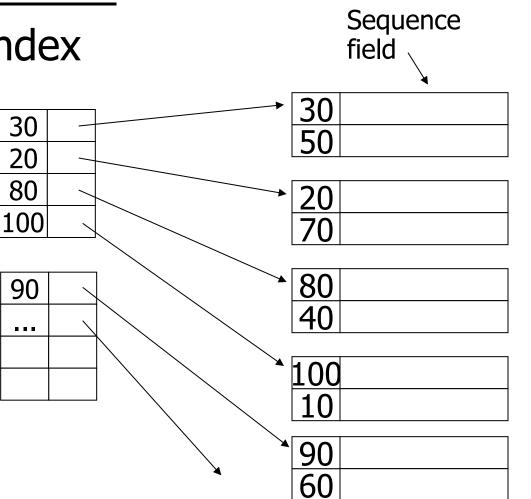
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• Sparse index

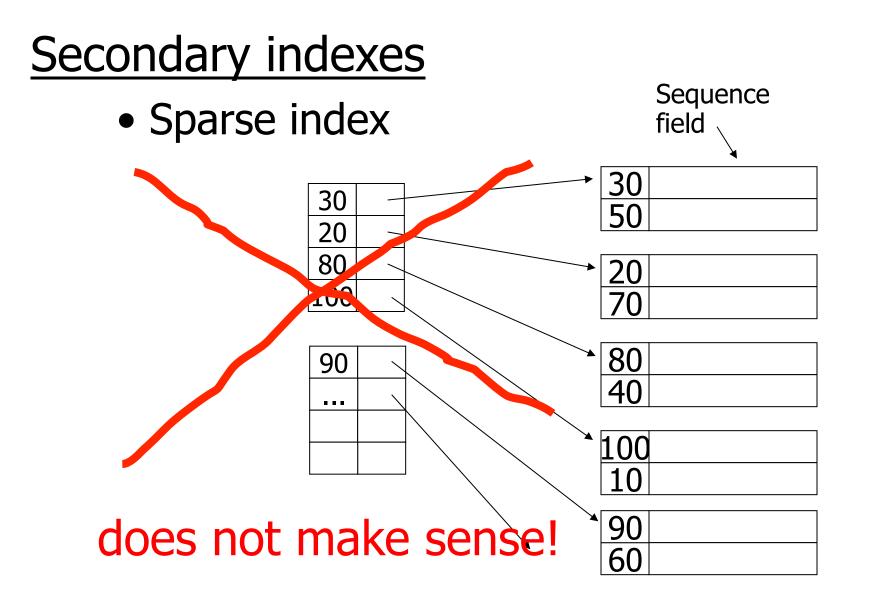




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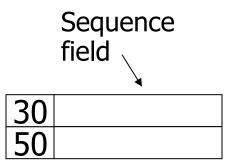
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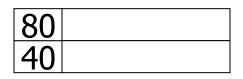


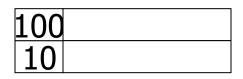
Secondary indexes

• Dense index









90	
60	



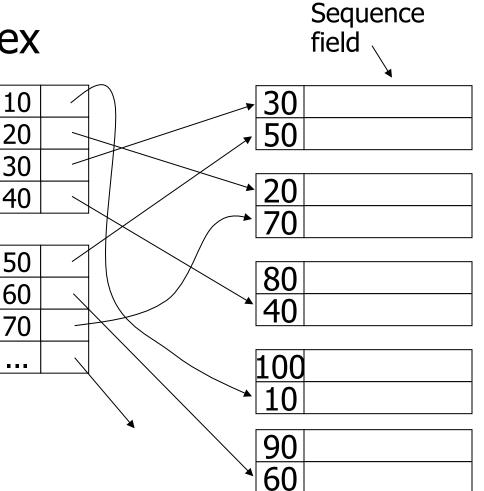
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Secondary indexes

• Dense index



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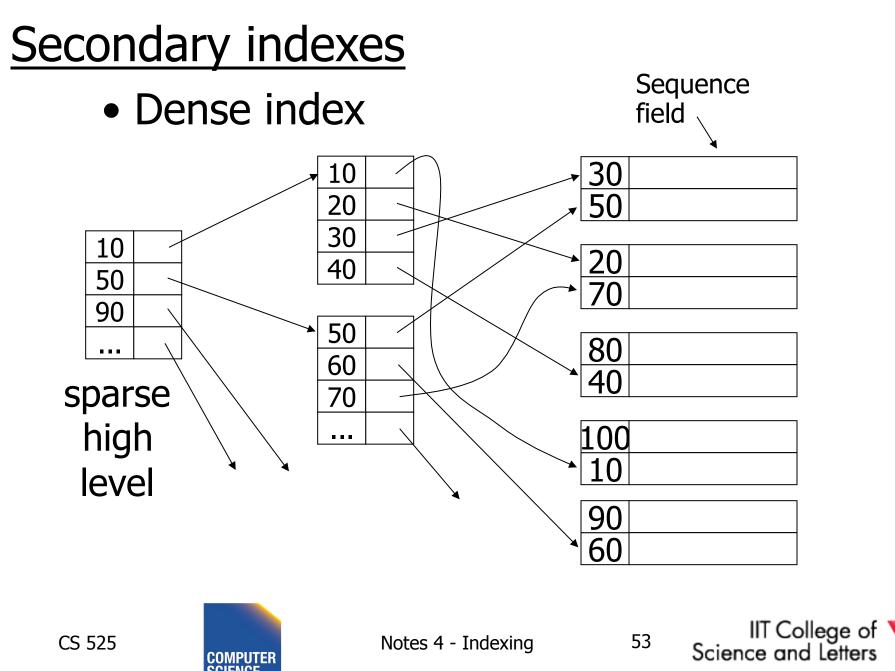


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With secondary indexes:

- Lowest level is dense
- Other levels are sparse

<u>Also:</u> Pointers are record pointers (not block pointers; not computed)

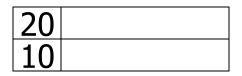


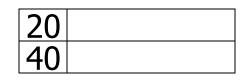
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30	
40	



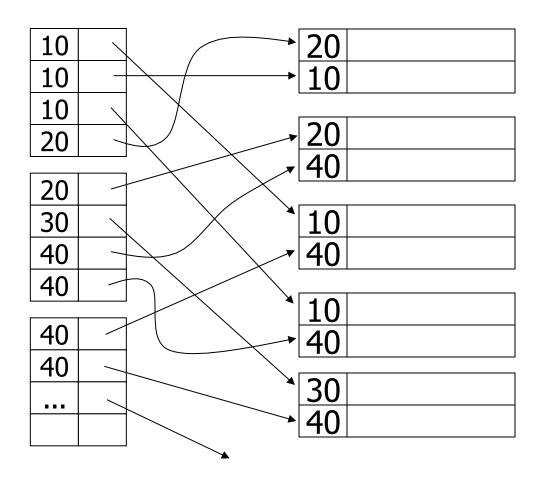
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one option...





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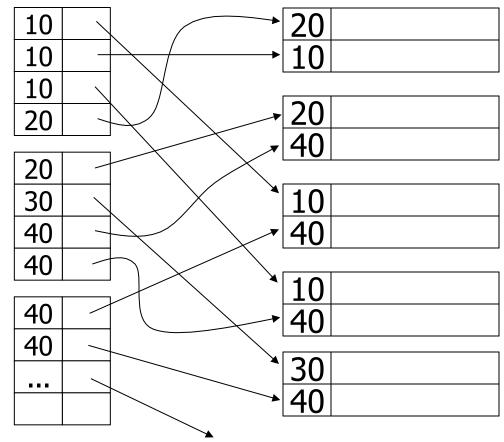


one option...

Problem: excess overhead!

- disk space
- search time

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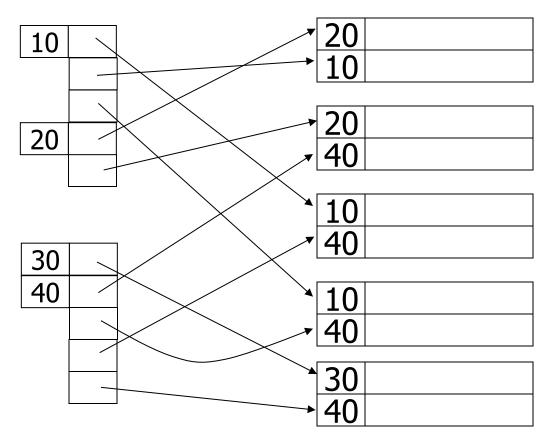




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another option...





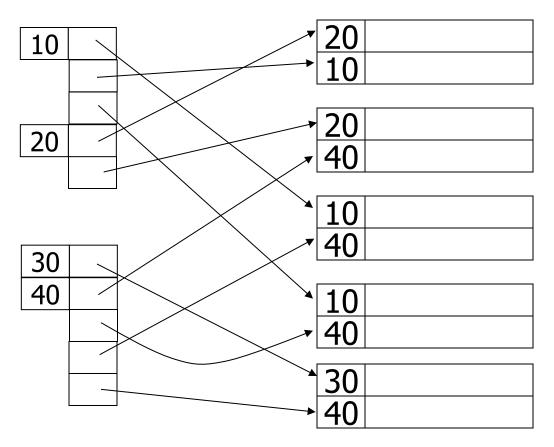
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another option...

Problem: variable size records in index!

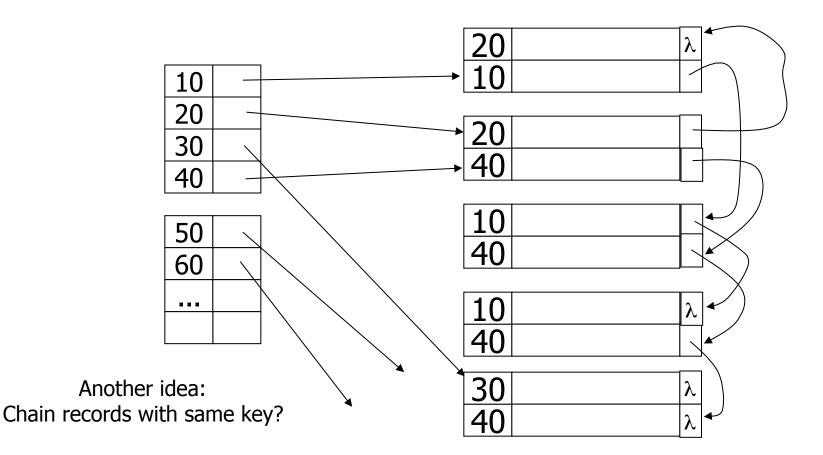
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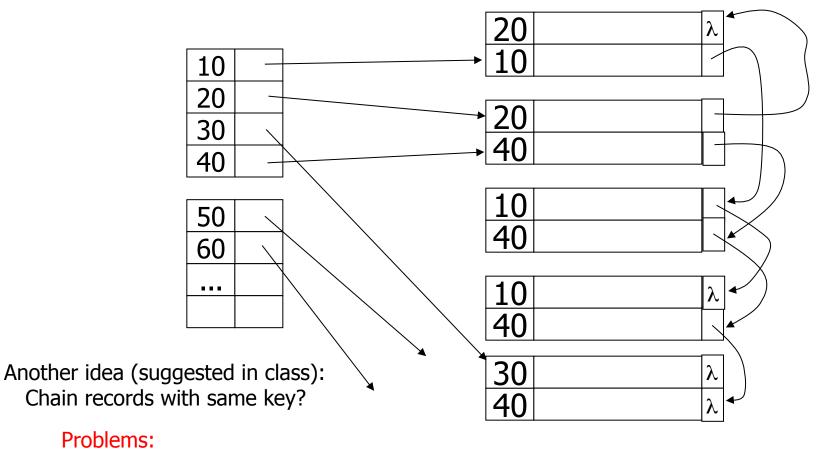




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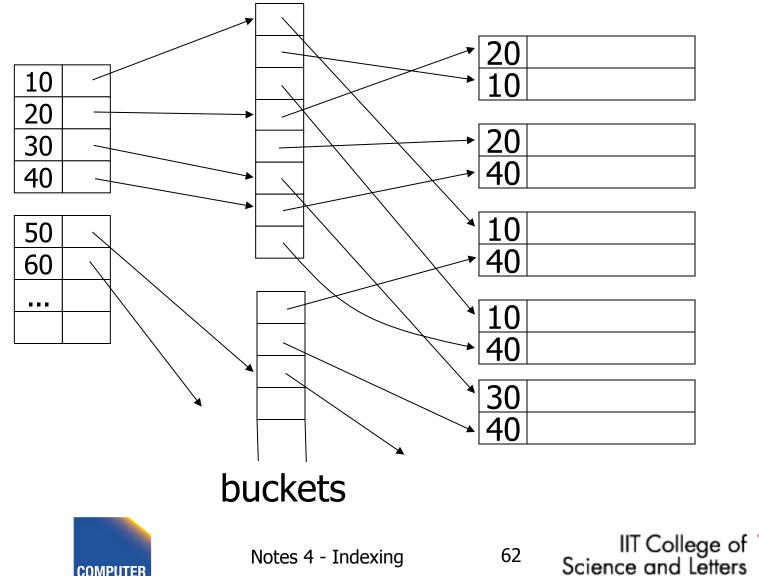
- Need to add fields to records
- Need to follow chain to know records





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Why "bucket" idea is useful

IndexesRecordsName: primaryEMP (name,dept,floor,...)Dept: secondaryFloor: secondary

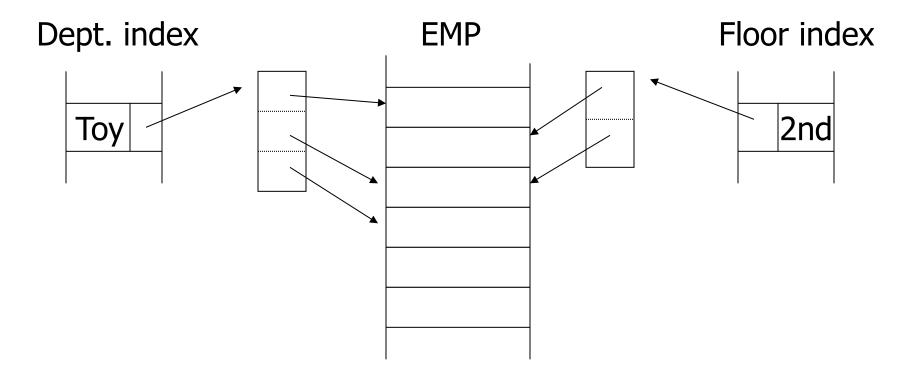


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Query: Get employees in (Toy Dept) ^ (2nd floor)



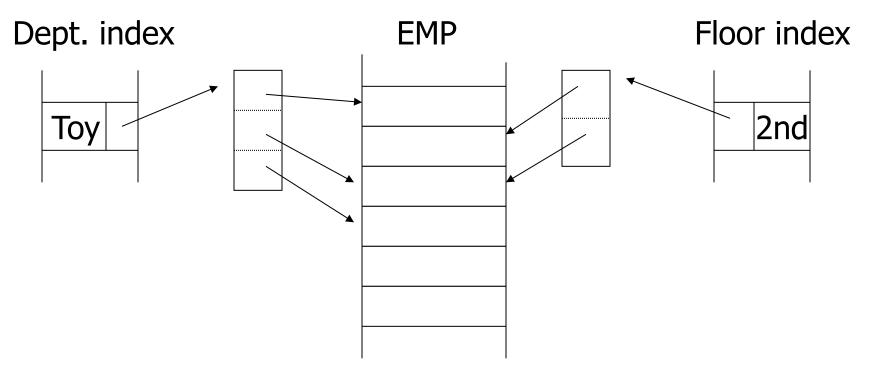


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Query: Get employees in (Toy Dept) $_{\wedge}$ (2nd floor)



→ Intersect toy bucket and 2nd Floor bucket to get set of matching EMP's

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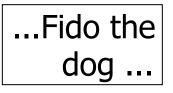
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This idea used in text information retrieval

Documents

...the cat is fat ...

...was raining cats and dogs...





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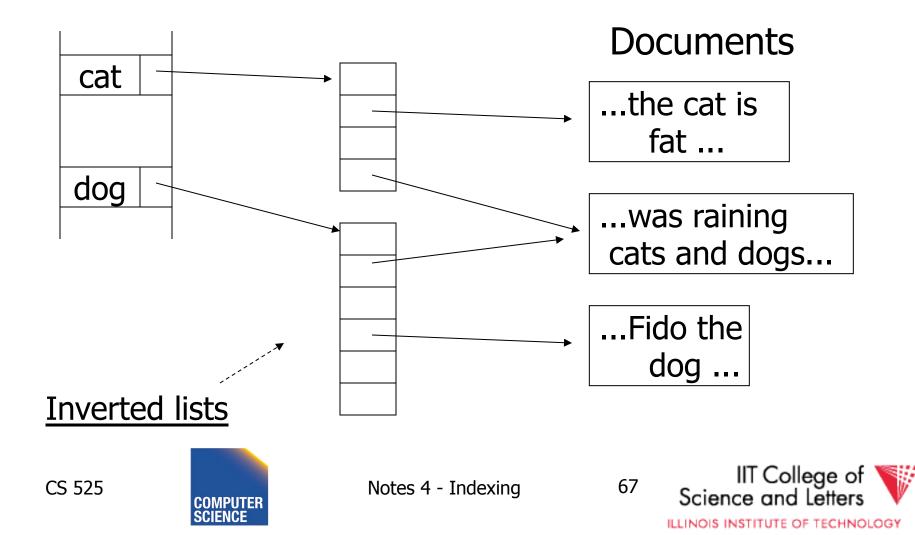
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This idea used in text information retrieval



IR QUERIES

- Find articles with "cat" and "dog"
- Find articles with "cat" or "dog"
- Find articles with "cat" and not "dog"



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Summary so far

- Conventional index
 - Basic Ideas: sparse, dense, multi-level...
 - Duplicate Keys
 - Deletion/Insertion
 - Secondary indexes
 - Buckets of Postings List



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Conventional indexes

Advantage:

- Simple
- Index is sequential file good for scans

Disadvantage:

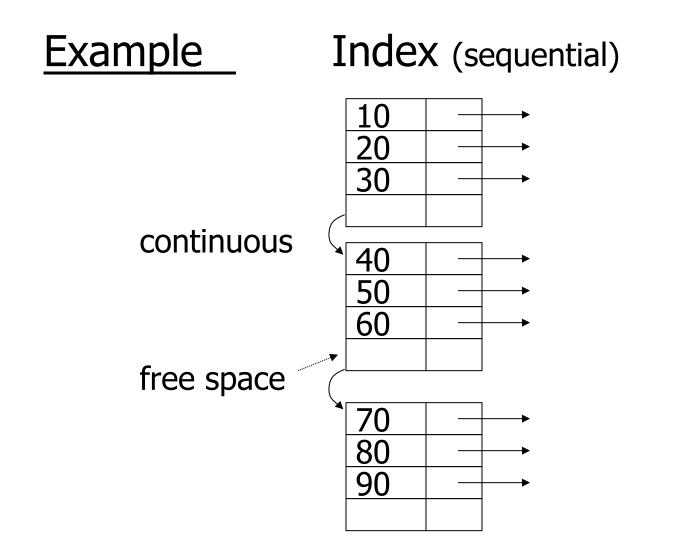
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- Inserts expensive, and/or
- Lose sequentiality & balance



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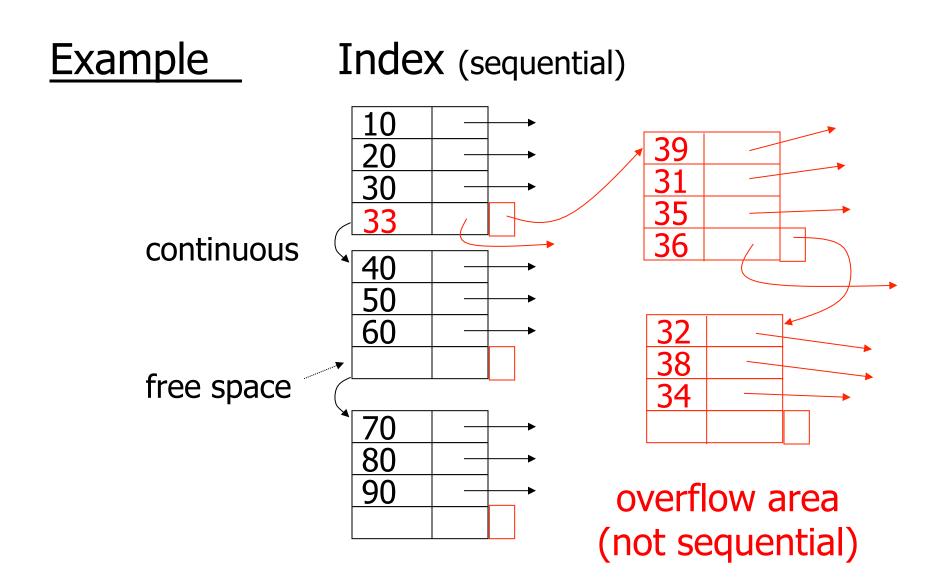




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Outline:

- Conventional indexes
- B-Trees \Rightarrow NEXT
- Hashing schemes
- Advanced Index Techniques



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- NEXT: Another type of index
 - Give up on sequentiality of index
 - Try to get "balance"



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B+-tree Motivation

- Tree indices are pretty efficient
 - E.g., binary search tree
 - Average case O(log(n)) lookup
- However
 - Unclear how to map to disk (index larger than main memory, loading partial index)
 - Worst-case O(n) lookup





B+-tree Properties

- Large nodes:
 - Node size is multiple of block size
 - -> small number of levels
 - -> simple way to map index to disk
 - -> many keys per node
- Balance:

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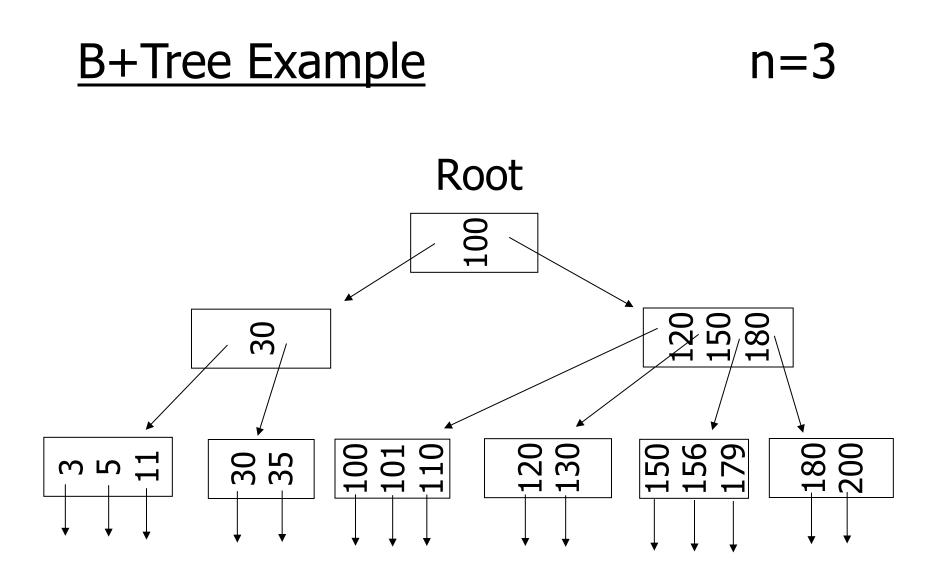
- Require all nodes to be more than X% full
- -> for n records guaranteed only logarithmically many levels
- --> log(n) worst-case performance



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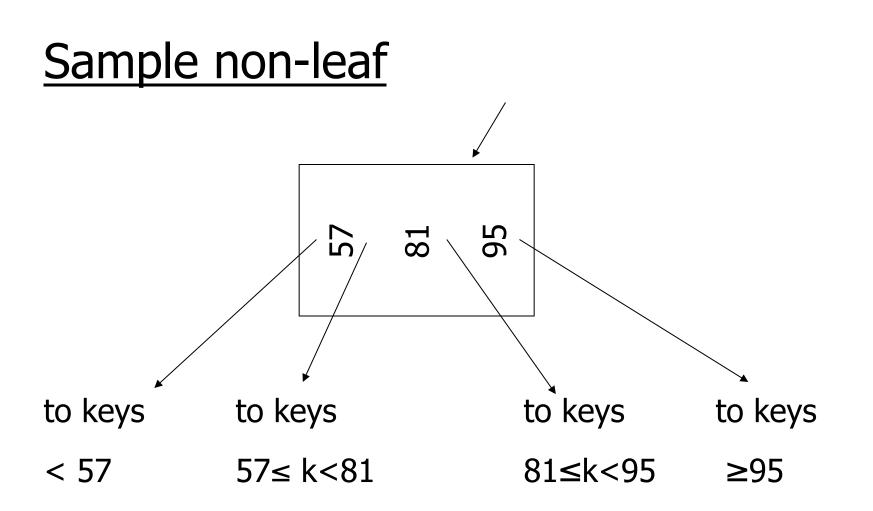




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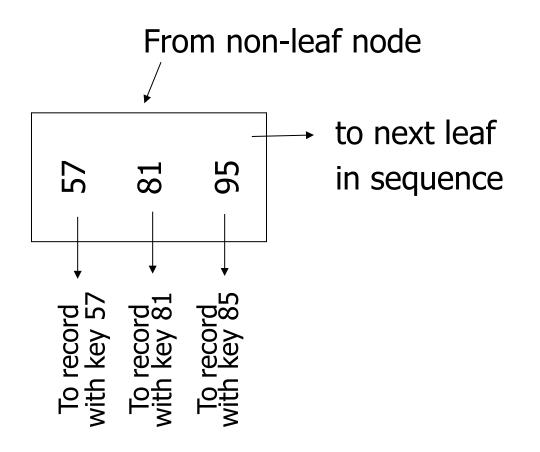




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Sample leaf node:





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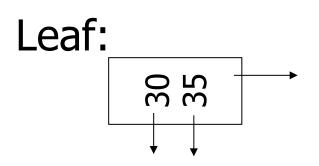
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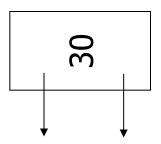
In textbook's notation

n=3



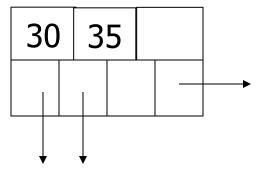
Non-leaf:

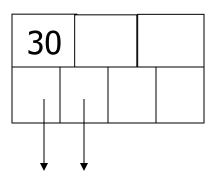
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Size of nodes:

n+1 pointers n keys



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Don't want nodes to be too empty

• Use at least (balance)

Non-leaf: [(n+1)/2] pointers

Leaf: $\lfloor (n+1)/2 \rfloor$ pointers to data



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n=3 Full node min. node Non-leaf 120 150 180 30 counts even if null Leaf 30 35 11 u u



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B+tree rules tree of order n

(1)All leaves at same lowest level (balanced tree)

-> guaranteed worst-case complexity for operations on the index

(2) Pointers in leaves point to records except for "sequence pointer"



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(3) Number of pointers/keys for B+tree

	Max ptrs	Max keys	Min ptrs→data	Min keys
Non-leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]- 1
Leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]
Root	n+1	n	1	1



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Search Algorithm

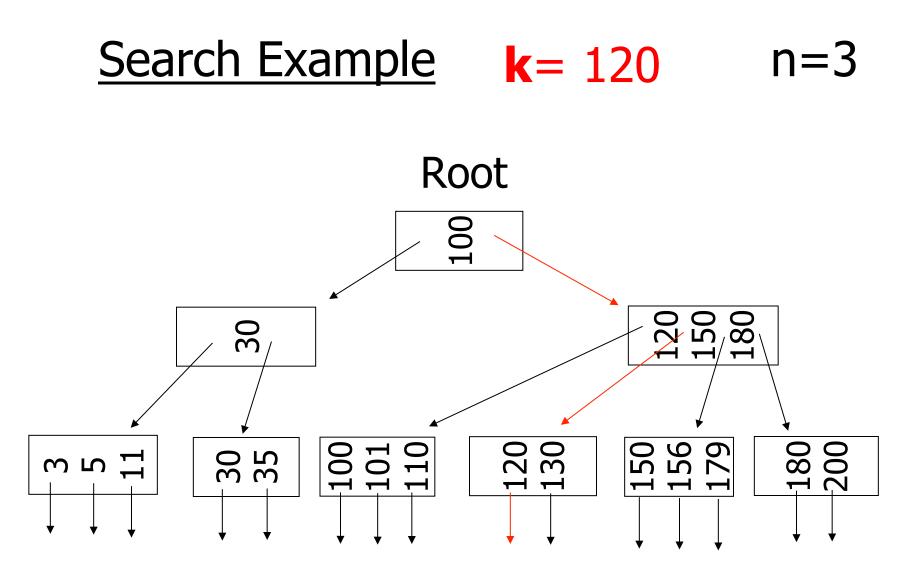
- Search for key ${\boldsymbol k}$
- Start from root until leaf is reached
- For current node find i so that
 - $-\text{Key}[i] \le \mathbf{k} \le \text{Key}[i + 1]$
 - Follow i+1th pointer
- If current node is leaf return pointer to record or fail (no such record in tree)



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Notes 4 - Indexing







Notes 4 - Indexing



Remarks Search

- If **n** is large, e.g., 500
- Keys inside node are sorted
- -> use binary search to find **I**
- Performance considerations
 - Linear search O(n)
 - Binary search $O(\log_2(n))$



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Insert into B+tree

(a) simple case

space available in leaf

(b) leaf overflow
(c) non-leaf overflow
(d) new root

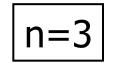


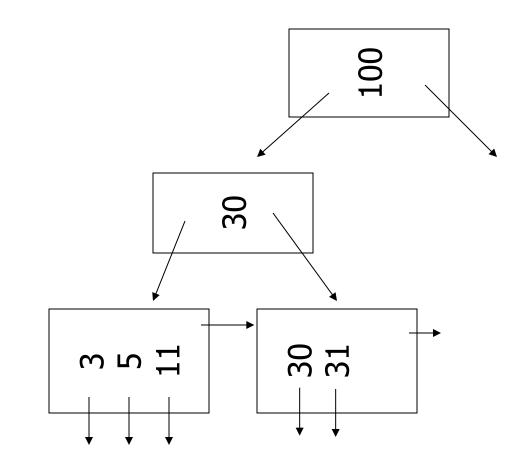
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(a) Insert key = 32





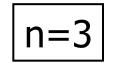


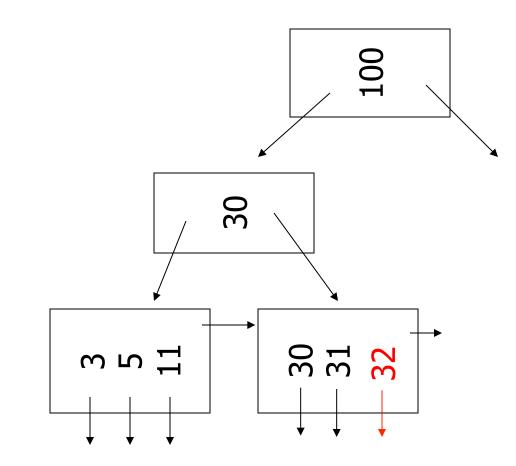
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Notes 4 - Indexing



(a) Insert key = 32





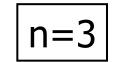


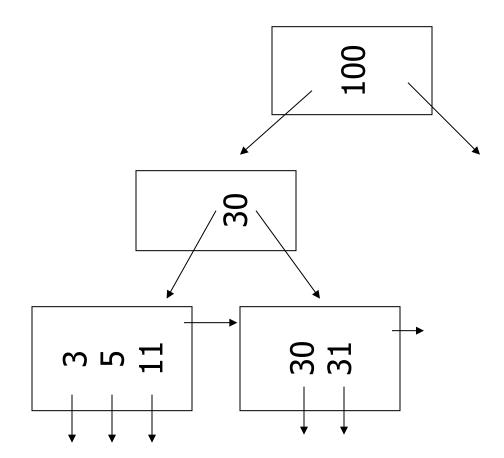
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Notes 4 - Indexing









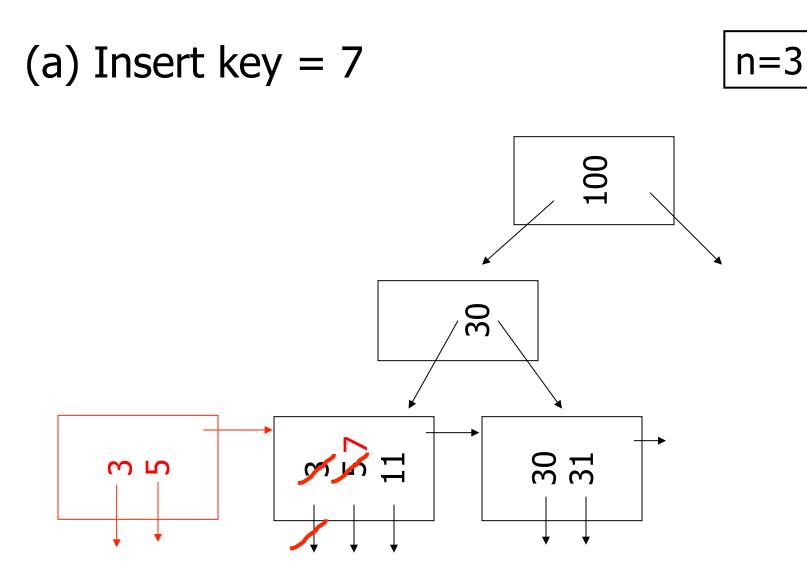


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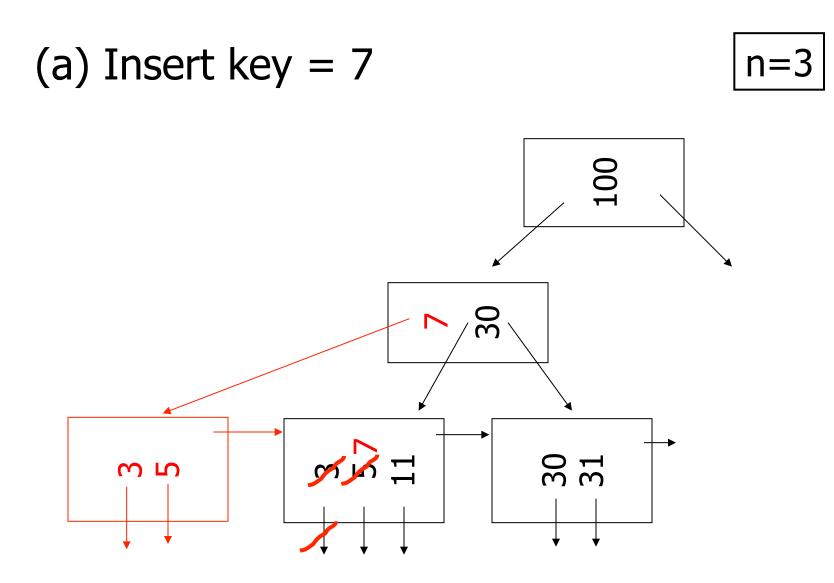
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Notes 4 - Indexing

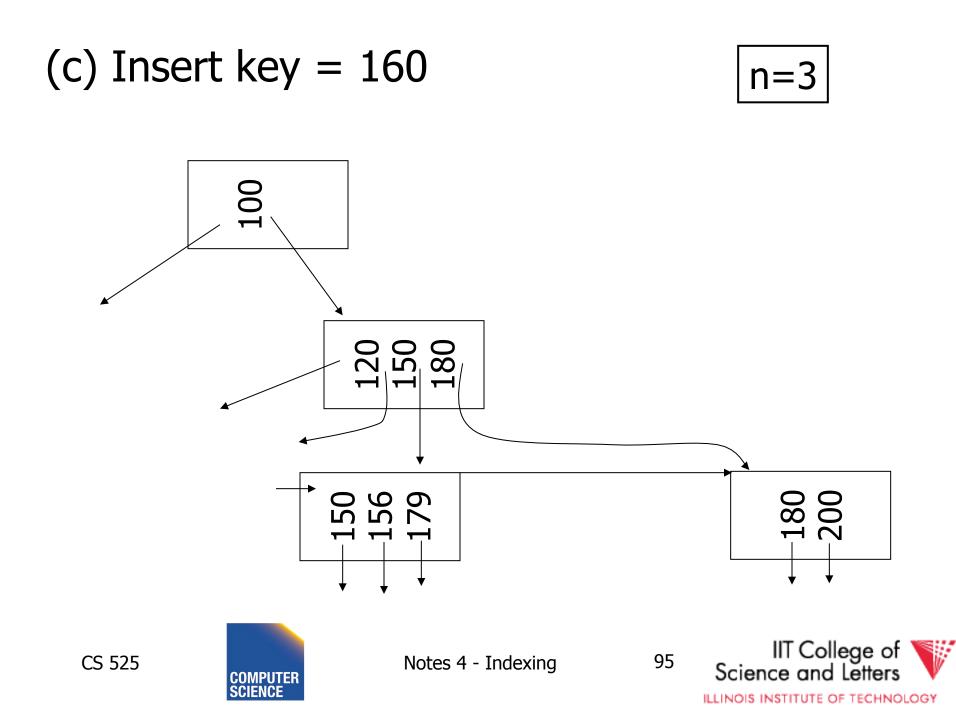


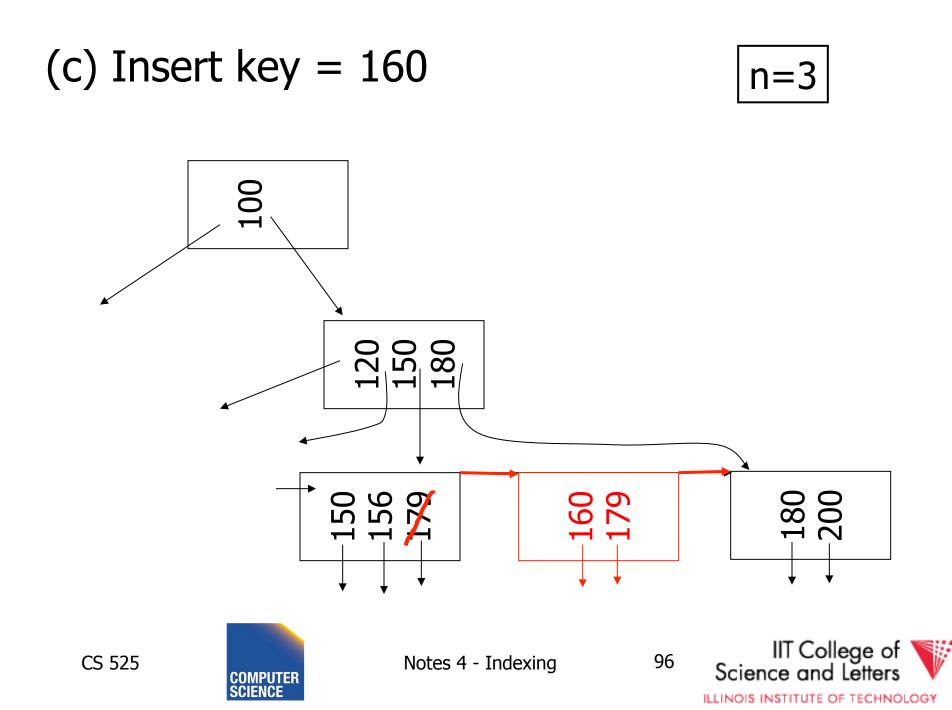


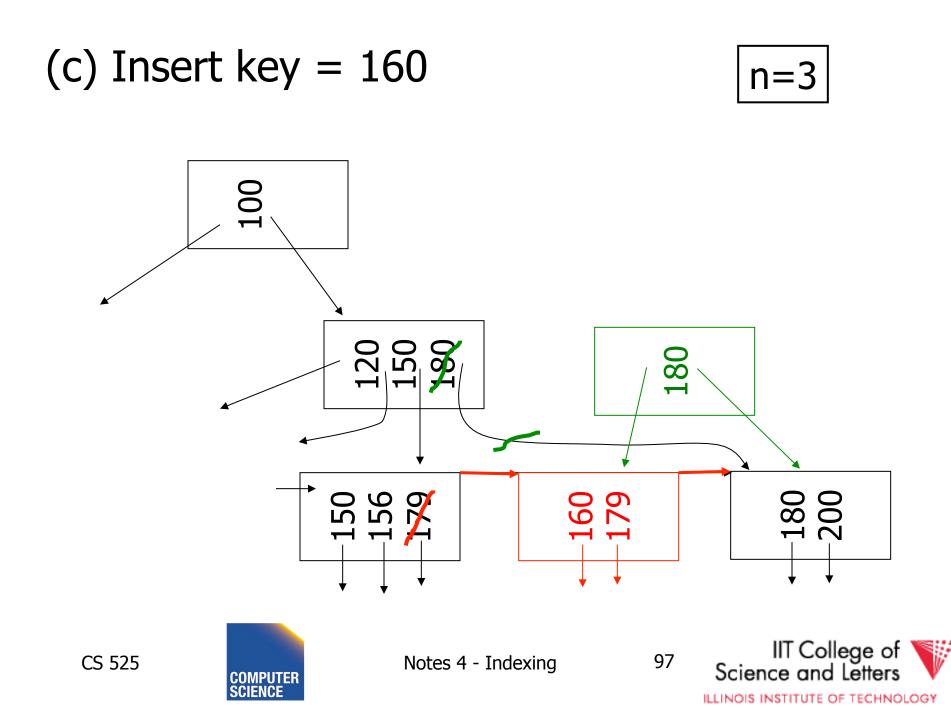


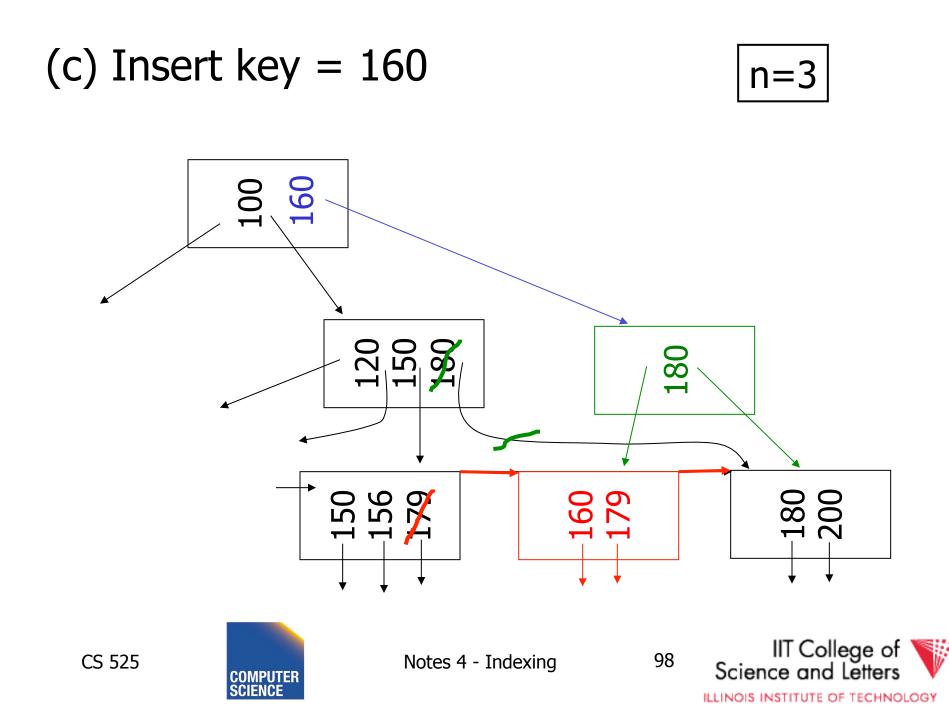
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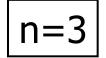


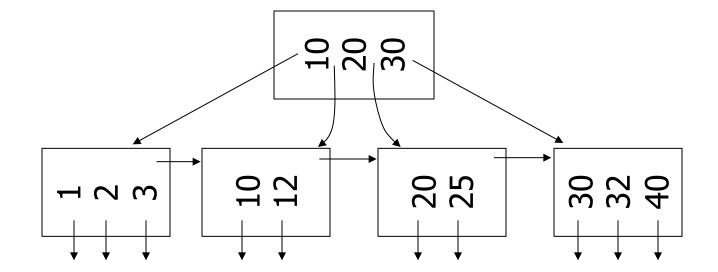






(d) New root, insert 45





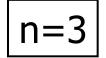


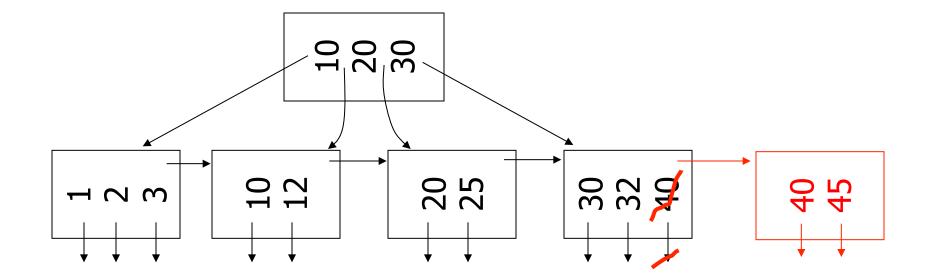
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(d) New root, insert 45





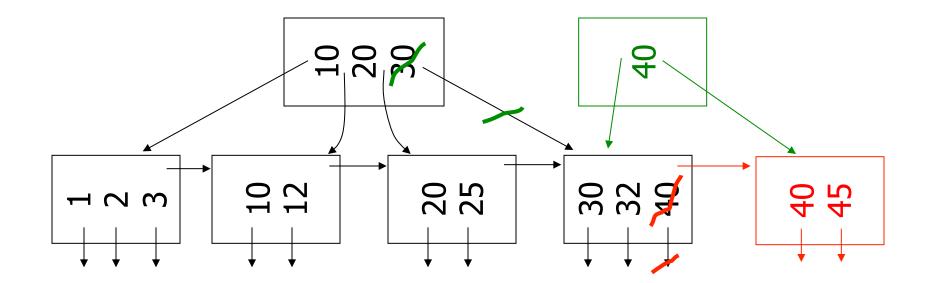


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(d) New root, insert 45

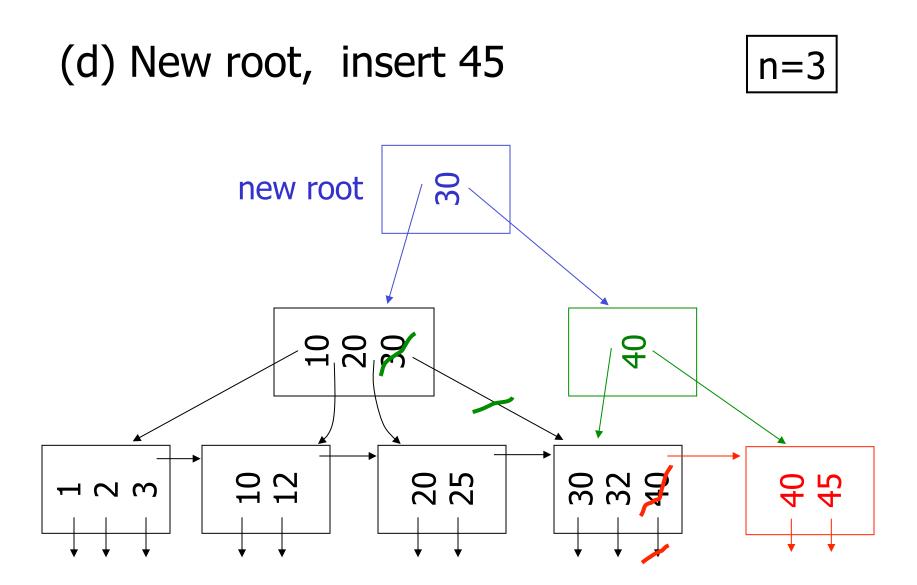




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Notes 4 - Indexing







Notes 4 - Indexing



Insertion Algorithm

- Insert Record with key ${\bf k}$
- Search leaf node for ${\boldsymbol k}$
 - Leaf node has at least one space
 - Insert into leaf
 - Leaf is full
 - Split leaf into two nodes (new leaf)
 - Insert new leaf's smallest key into parent



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Insertion Algorithm cont.

Non-leaf node is full

- Split parent
- Insert median key into parent
- Root is full
 - Split root
 - Create new root with two pointers and single key
- -> B-trees grow at the root



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Notes 4 - Indexing



Deletion from B+tree

(a) Simple case - no example
(b) Coalesce with neighbor (sibling)
(c) Re-distribute keys
(d) Cases (b) or (c) at non-leaf

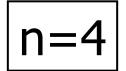


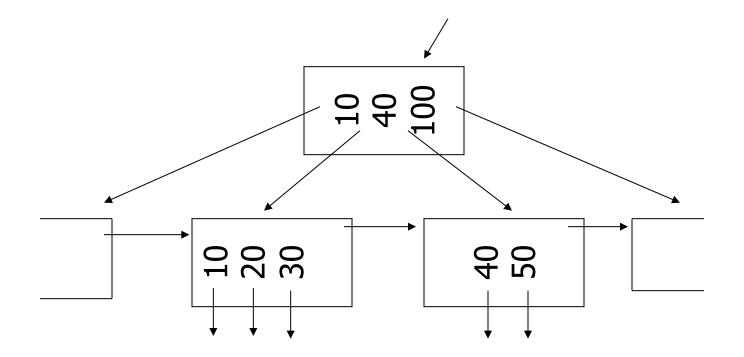
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(b) Coalesce with sibling – Delete 50





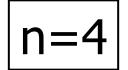


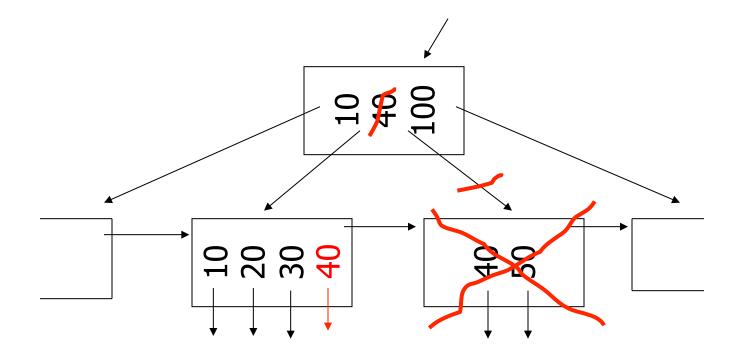
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(b) Coalesce with sibling – Delete 50





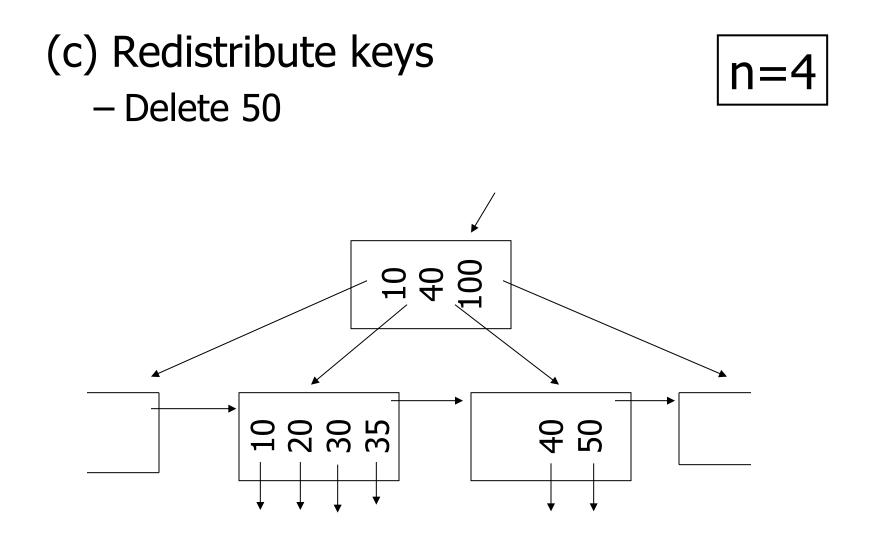


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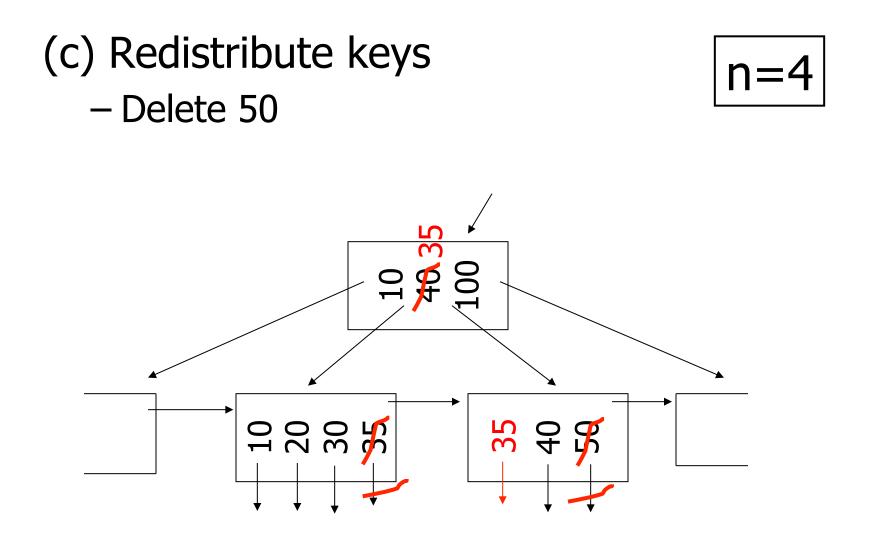






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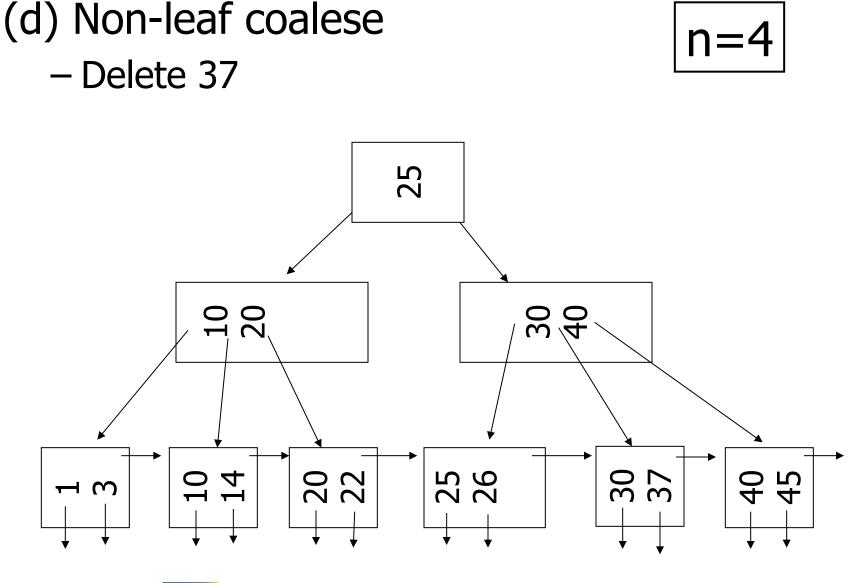






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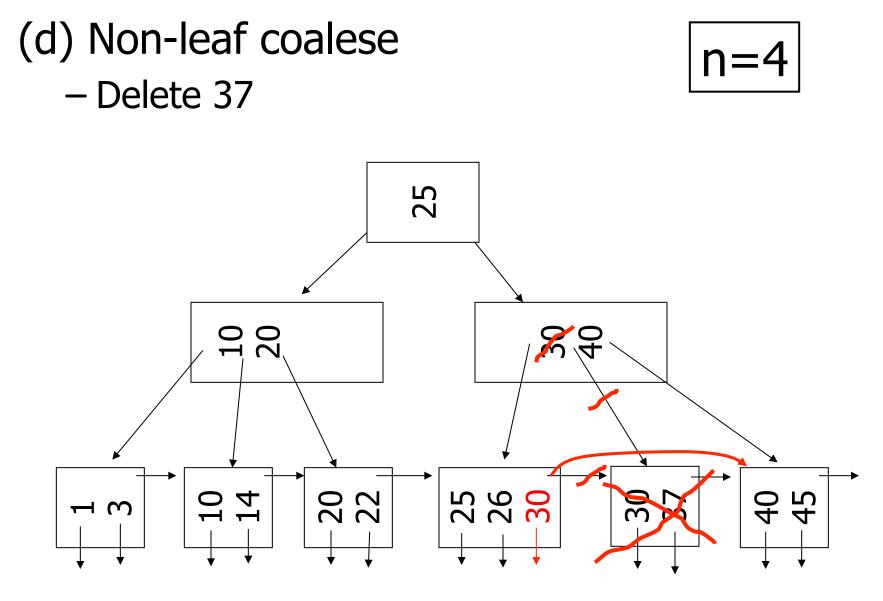






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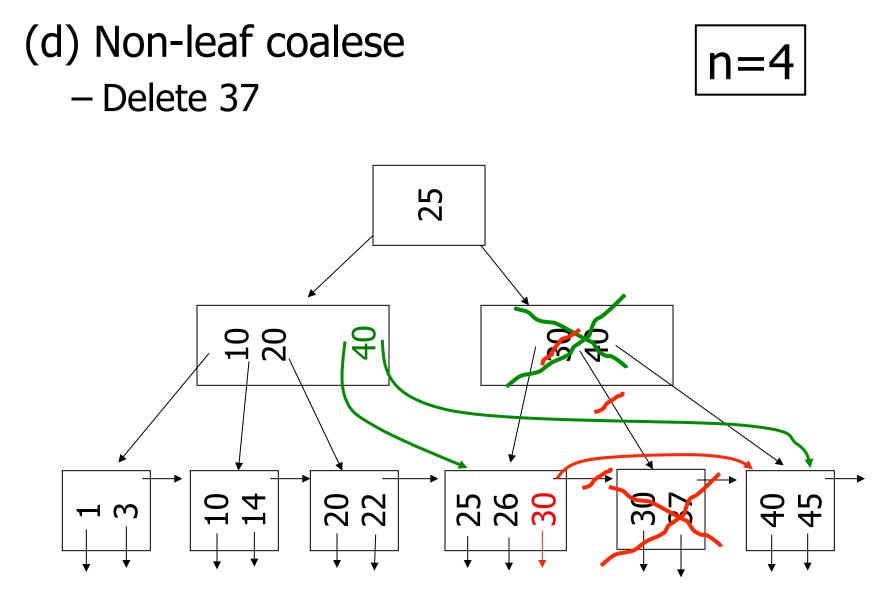






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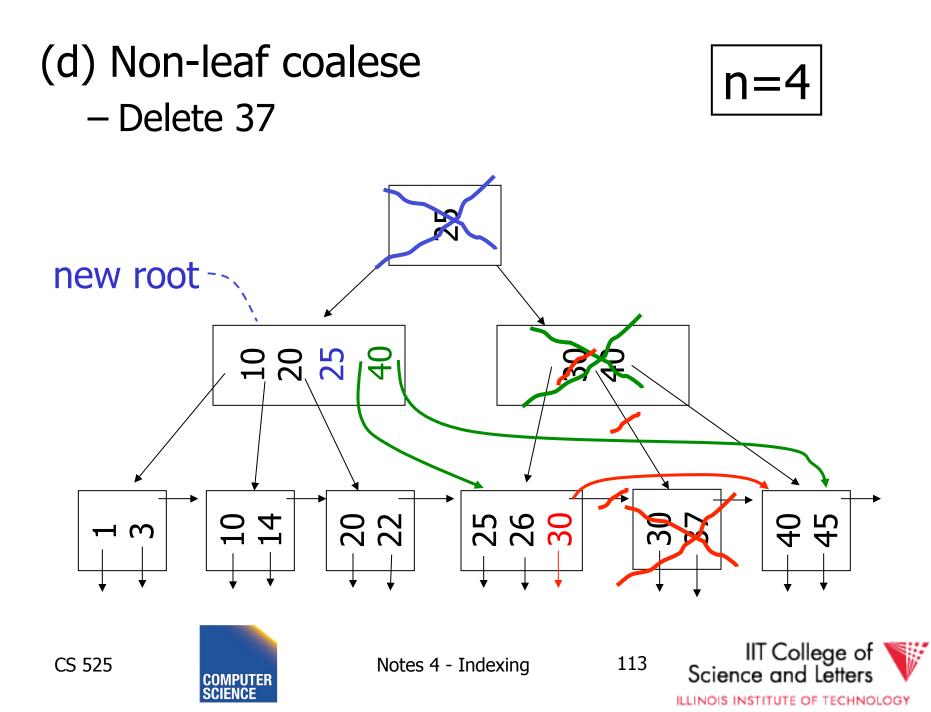
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Notes 4 - Indexing





Deletion Algorithm

- Delete record with key ${\bf k}$
- Search leaf node for ${\boldsymbol k}$
 - Leaf has more than min entries
 - Remove from leaf
 - Leaf has min entries
 - Try to borrow from sibling
 - One direct sibling has more min entries
 - Move entry from sibling and adapt key in parent



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Deletion Algorithm cont.

- Both direct siblings have min entries
 - Merge with one sibling
 - Remove node or sibling from parent
 - ->recursive deletion
- Root has two children that get merged – Merged node becomes new root



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<u>B+tree deletions in practice</u>

– Often, coalescing is not implemented

- Too hard and not worth it!
- Assumption: nodes will fill up in time again



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Notes 4 - Indexing



Comparison: B-trees vs. static indexed sequential file

Ref #1:Held & Stonebraker"B-Trees Re-examined"CACM, Feb. 1978



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Ref # 1 claims:

- Concurrency control harder in B-Trees
 - B-tree consumes more space

```
For their comparison:
block = 512 bytes
key = pointer = 4 bytes
4 data records per block
```

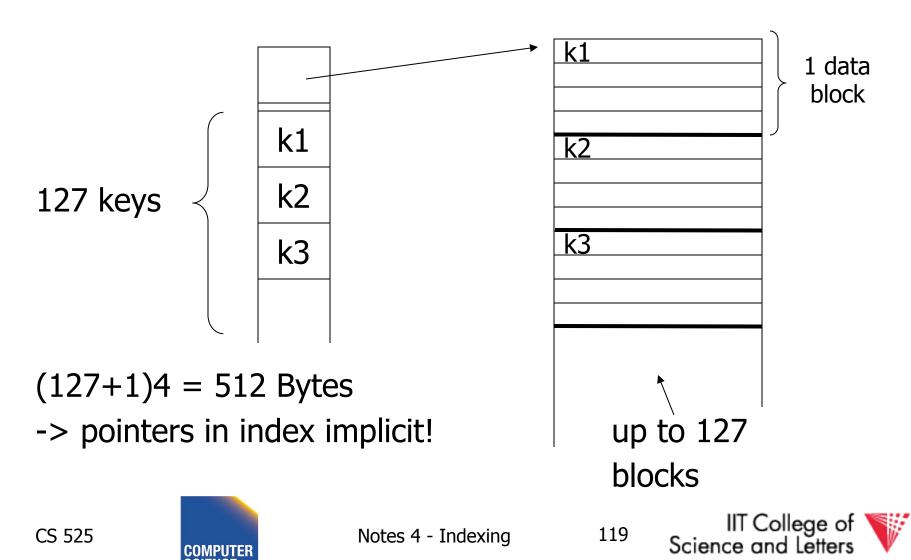


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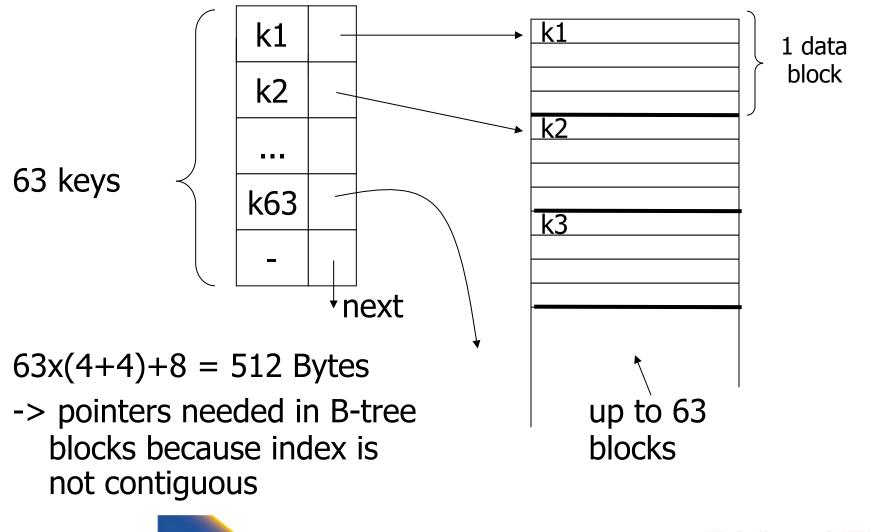
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Example: 1 block static index



Example: 1 block B-tree



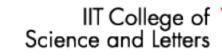




Size comp	arison	Ref. #1		
<u>Static I</u> # data blocks	<u>index</u> height	B-tree # data blocks	neight	
2 -> 127 128 -> 16,129 16,130 -> 2,048	2 3 ,383 4	2 -> 63 64 -> 3968 3969 -> 250,047 250,048 -> 15,752,963	2 3 4 1 5	



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Ref. #1 analysis claims

- For an 8,000 block file, $\begin{cases} after 32,000 \text{ inserts} \\ after 16,000 \text{ lookups} \\ \Rightarrow \text{ Static index saves enough accesses} \end{cases}$
 - to allow for reorganization



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Ref. #1 analysis claims

- For an 8,000 block file, $\begin{cases} after 32,000 \text{ inserts} \\ after 16,000 \text{ lookups} \\ \Rightarrow \text{ Static index saves enough accesses} \end{cases}$
 - to allow for reorganization



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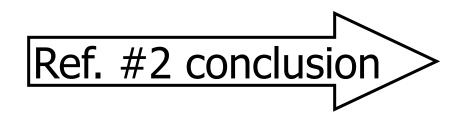
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Ref #2: M. Stonebraker,

"Retrospective on a database system," TODS, June 1980



B-trees better!!

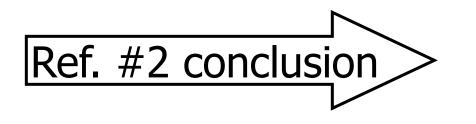


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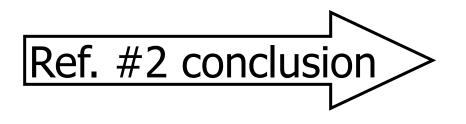


- DBA does not know <u>when</u> to reorganize
- DBA does not know <u>how full</u> to load pages of new index



Notes 4 - Indexing





B-trees better!!

- Buffering
 - B-tree: has fixed buffer requirements
 - Static index: must read several overflow blocks to be efficient (large & variable size

size needed for this)



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• Speaking of buffering... Is LRU a good policy for B+tree buffers?



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- Speaking of buffering... Is LRU a good policy for B+tree buffers?
 - \rightarrow Of course not!
 - → Should try to keep root in memory at all times

(and perhaps some nodes from second level)



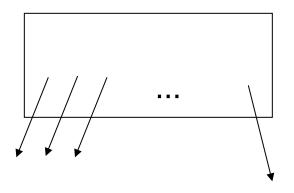
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Interesting problem:

For B+tree, how large should *n* be?



n is number of keys / node



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Sample assumptions:

(1) Time to read node from disk is (S+T*n*) msec.



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Sample assumptions:

(1) Time to read node from disk is (S+T*n*) msec.

(2) Once block in memory, use binary search to locate key: (a + b LOG₂ n) msec.

For some constants *a*,*b*; Assume a << S



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Sample assumptions:

(1) Time to read node from disk is (S+T*n*) msec.

(2) Once block in memory, use binary search to locate key:
 (a + b LOG₂ n) msec.

For some constants *a*,*b*; Assume a << S

(3) Assume B+tree is full, i.e.,
 # nodes to examine is LOG_n N
 where N = # records

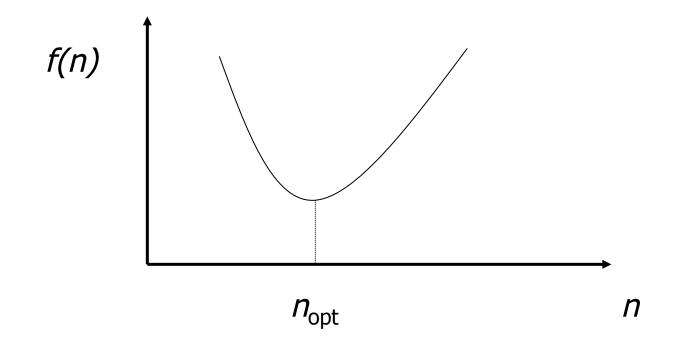


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➤Can get: f(n) = time to find a record





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► FIND n_{opt} by f'(n) = 0

Answer is $n_{opt} =$ "few hundred"



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► FIND n_{opt} by f'(n) = 0

Answer is n_{opt} = "few hundred"

\rightarrow What happens to n_{opt} as

- Disk gets faster?
- CPU get faster?
- Memory hierarchy?



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Variation on B+tree: B-tree (no +)

• Idea:

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Avoid duplicate keys

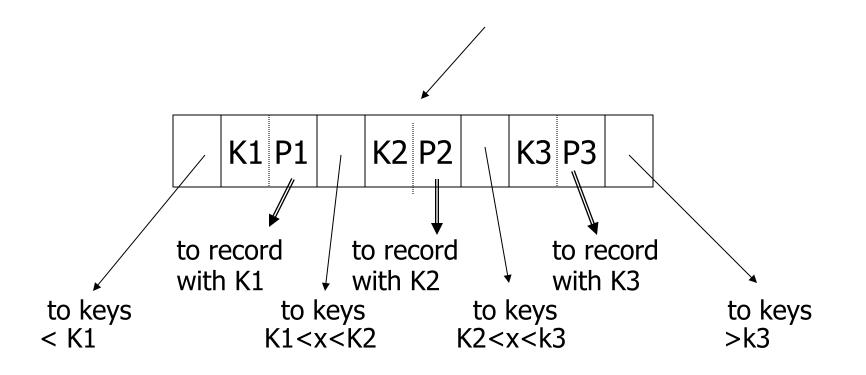
- Have record pointers in non-leaf nodes



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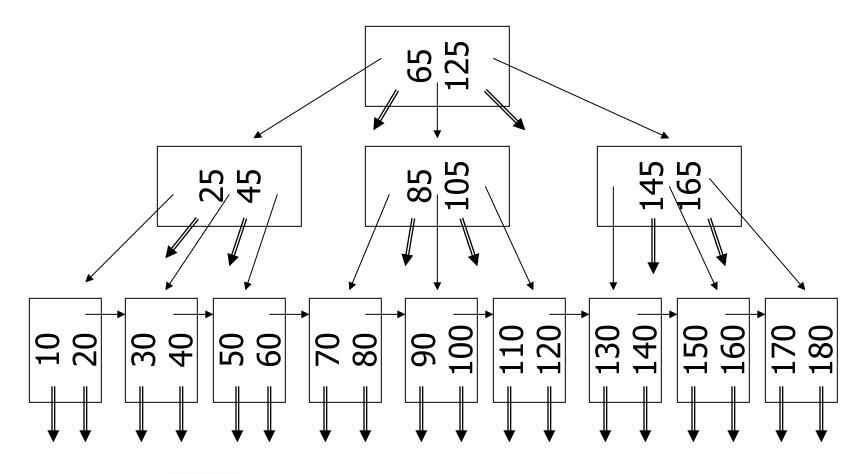


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B-tree example

n=2



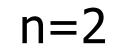


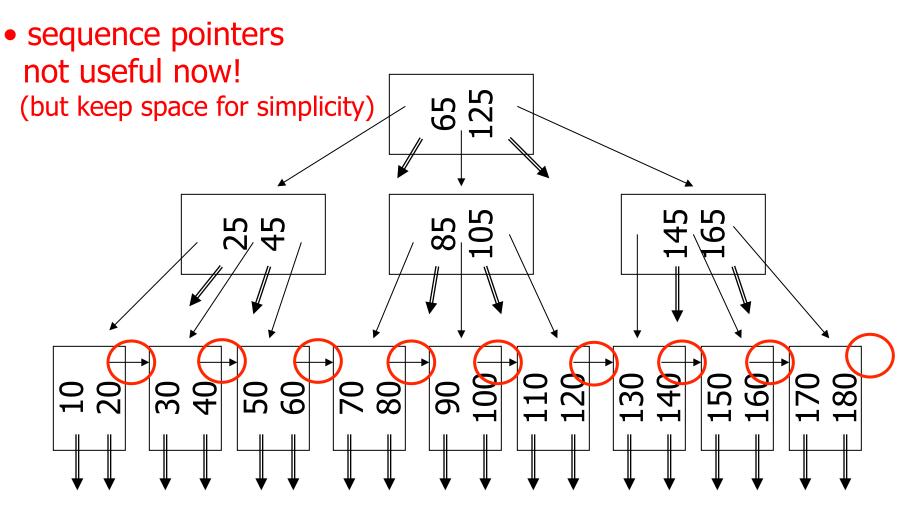
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B-tree example







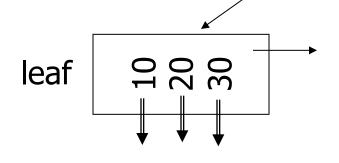
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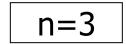
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Note on inserts

• Say we insert record with key = 25







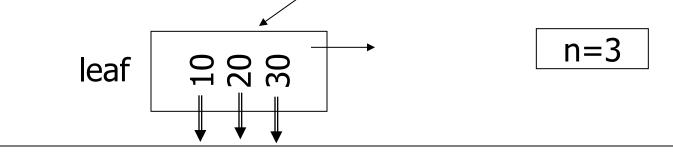
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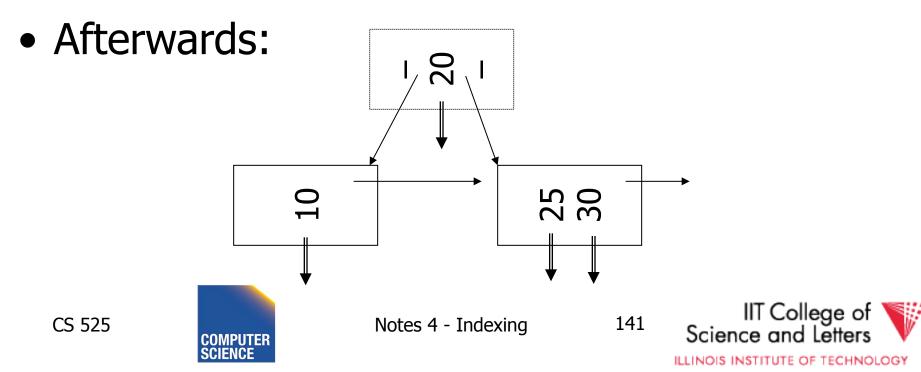
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Note on inserts

• Say we insert record with key = 25





So, for B-trees:

	MAX			MIŅ		
	Tree Ptrs	Rec Ptrs	Keys	Tree Ptrs	Rec Ptrs	Keys
Non-leaf non-root	n+1	n	n		[(n+1)/2]-1	[(n+1)/2]-1
Leaf non-root	1	n	n	1	[n/2]	[n/2]
Root non-leaf	n+1	n	n	2	1	1
Root Leaf	1	n	n	1	1	1



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Tradeoffs:

☺ B-trees have faster lookup than B+trees

⊗ in B-tree, non-leaf & leaf different sizes⊗ in B-tree, deletion more complicated



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Tradeoffs:

☺ B-trees have faster lookup than B+trees

in B-tree, non-leaf & leaf different sizes
 in B-tree, deletion more complicated

➡ B+trees preferred!



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But note:

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• If blocks are fixed size

(due to disk and buffering restrictions) Then lookup for B+tree is actually better!!



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Example:

- Pointers 4 bytes
- Keys 4 bytes
- Blocks 100 bytes (just example)
- Look at full 2 level tree



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B-tree:

Root has 8 keys + 8 record pointers + 9 son pointers = 8x4 + 8x4 + 9x4 = 100 bytes



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B-tree:

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Root has 8 keys + 8 record pointers + 9 son pointers = 8x4 + 8x4 + 9x4 = 100 bytes

Each of 9 sons: 12 rec. pointers (+12 keys) = 12x(4+4) + 4 = 100 bytes



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B-tree:

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Root has 8 keys + 8 record pointers + 9 son pointers = 8x4 + 8x4 + 9x4 = 100 bytes

Each of 9 sons: 12 rec. pointers (+12 keys) = 12x(4+4) + 4 = 100 bytes

<u>2-level B-tree, Max # records</u> = 12x9 + 8 = 116



Notes 4 - Indexing





<u>Root</u> has 12 keys + 13 son pointers = 12x4 + 13x4 = 100 bytes



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B+tree:

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$\frac{\text{Root}}{\text{Hoot}} \text{ has } 12 \text{ keys} + 13 \text{ son pointers}$ = 12x4 + 13x4 = 100 bytes

Each of 13 sons: 12 rec. ptrs (+12 keys) = 12x(4 + 4) + 4 = 100 bytes



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B+tree:

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<u>Root</u> has 12 keys + 13 son pointers = 12x4 + 13x4 = 100 bytes

Each of 13 sons: 12 rec. ptrs (+12 keys) = 12x(4 + 4) + 4 = 100 bytes

$\frac{2 \text{-level B+tree, Max # records}}{= 13 \text{x} 12 = 156}$



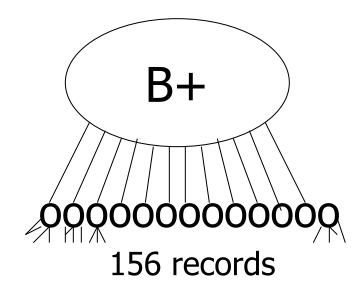
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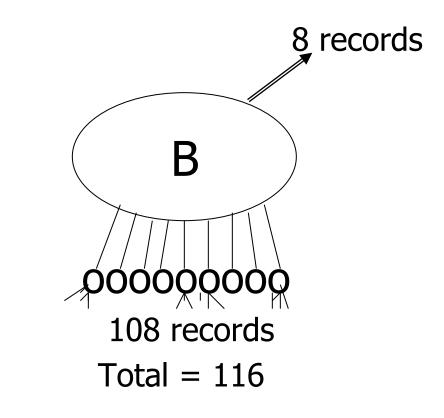
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So...

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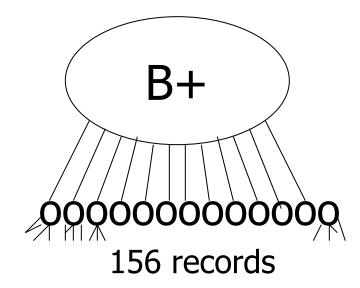


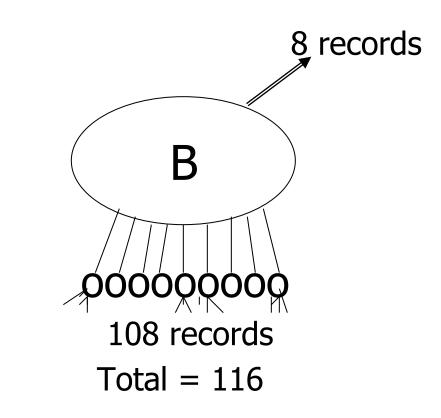


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So...





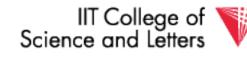
- Conclusion:
 - For fixed block size,
 - B+ tree is better because it is bushier





Notes 4 - Indexing





Additional B-tree Variants

• B*-tree

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- Internal notes have to be 2/3 full



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An Interesting Problem...

- What is a good index structure when:
 - records tend to be inserted with keys that are larger than existing values? (e.g., banking records with growing data/time)
 - we want to remove older data



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One Solution: Multiple Indexes

• Example: I1, I2

day	days indexed I1	days indexed I2
10	1,2,3,4,5	6,7,8,9,10
11	11,2,3,4,5	6,7,8,9,10
12	11,12,3,4,5	6,7,8,9,10
13	11,12,13,4,5	6,7,8,9,10

advantage: deletions/insertions from smaller index
disadvantage: query multiple indexes

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Another Solution (Wave Indexes)

day	I1	I2	I3	I4
10	1,2,3	4,5,6	7,8,9	10
11	1,2,3	4,5,6	7,8,9	10,11
12	1,2,3	4,5,6	7,8,9	10,11, 12
13	13	4,5,6	7,8,9	10,11, 12
14	13,14	4,5,6	7,8,9	10,11, 12
15	13,14,15	4,5,6	7,8,9	10,11, 12
16	13,14,15	16	7,8,9	10,11, 12

advantage: no deletionsdisadvantage: approximate windows



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Notes 4 - Indexing



Concurrent Access To B-trees

- Multiple processes/threads accessing the B-tree
 - Can lead to corruption
- Serialize access to complete tree for updates
 - Simple
 - Unnecessary restrictive
 - Not feasible for high concurrency





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Lock Nodes

• One solution

- ReadWriteReadXWrite-
- Safe and unsafe updates of nodes
 - **Safe:** No ancestor of node will be effected by update
 - Unsafe: Ancestor may be affected
 - Can be determined locally

- Read and exclusive locks

– E.g., deletion is safe is node has more than n/2



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Notes 4 - Indexing



Lock Nodes

- Reading
 - Use standard search algorithm
 - Hold lock on current node
 - Release when navigating to child
- Writing
 - Lock each node on search for key
 - Release all locks on parents of node if the node is safe





Notes 4 - Indexing



Improvements?

- Try locking only the leaf for update
 - Let update use read locks and only lock leaf node with write lock
 - If leaf node is unsafe then use previous protocol
- Many more locking approaches have been proposed



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Outline/summary

- Conventional Indexes
 - Sparse vs. dense
 - Primary vs. secondary
- B trees

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- B+trees vs. B-trees
- B+trees vs. indexed sequential
- Hashing schemes --> Next
- Advanced Index Techniques



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