

CS 595 - Hot topics in database systems:

Data Provenance

I. Database Provenance

I.1 Provenance Models and Systems

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Excursion: Semirings

Commutative Monoids

- $(K, +, 0)$
- A set K
- An operation $K \rightarrow K$ (say $+$) with neutral element 0 :
 - $(a + b) + c = a + (b + c)$ (associativity)
 - $0 + a = a$ (neutral element)
 - $a + b = b + a$ (commutativity)

Example

- $(\mathbb{N}, +, 0)$ - Natural numbers addition
- $(\mathbb{N}, \times, 1)$ - Natural numbers multiplication
- $(\mathbb{B}, \wedge, true)$: $\mathbb{B} = \{true, false\}$ - Conjunction over boolean constants
- $(\mathbb{B}, \vee, false)$ - Disjunction over boolean constants

Excursion: Semirings

Commutative Semiring

- $(K, +, \times, 0, 1)$
- Set K with operations $+$ and \times (neutral elements 0 and 1)
- $(K, +, 0)$ and $(K, \times, 1)$ are commutative monoids
- $a \times (b + c) = (a \times b) + (a \times c)$ (Distributivity)
- $(a + b) \times c = (a \times c) + (b \times c)$ (Distributivity)
- $a \times 0 = 0 \times a = 0$ (multiplication with 0)

Example

- $(\mathbb{N}, +, \times, 0, 1)$ - Natural numbers with addition and multiplication
- $(\mathbb{B}, \vee, \wedge, \text{false}, \text{true})$ - Conjunctions and disjunctions over boolean constants

Free Objects

- Given an algebraic structure a free object is one with an homomorphism into all other objects of this type
 - E.g., the free commutative semiring is an structure with homomorphism into all other commutative semirings
- \Rightarrow The **free semiring** is the most general semiring
- \Rightarrow Only equivalences enforced by the structure being semiring can hold
 - For any additional equivalence: Find semiring where equivalence does not hold \Rightarrow No homomorphism! **contradiction**
- \Rightarrow Elements of free semiring are uninterpreted expressions
 - Placeholders for semiring elements
 - Do not interpret semiring operation

Interpretations of Semirings

Semiring Interpretations

- $(\mathbb{B}, \vee, \wedge, \text{false}, \text{true})$: $\mathbb{B} = \{\text{false}, \text{true}\}$: Tuples with true/false annotations \Rightarrow Set-semantics

Example

		R
		a
true		1
true		2

Relational Algebra for K -relations

Rationale

- Express relational algebra operators as semiring operations
- **Sanity checks:**
 - For $K = \mathbb{B}$ \Rightarrow same results (equivalences) as set-semantics
 - For $K = \mathbb{N}$ \Rightarrow same results (equivalences) as bag-semantics

Operator Definitions

Selection

- $(\sigma_C(R))(t) = R(t) \times C(t)$
- Selection predicate C is function $U - Tup \rightarrow \{0, 1\}$
 - Recall $a \times 0 = 0$ and $a \times 1 = a$

Projection

- $(\pi_A(R))(t) = \sum_{t=t'.A} R(t')$
 - $A \subseteq U$

Union

- $(R_1 \cup R_2)(t) = R_1(t) + R_2(t)$

Operator Definitions

Natural Join

- $(R_1 \bowtie R_2)(t) = R_1(t_1) \times R_2(t_2)$
 - $t_1 = t.U_1$
 - $t_2 = t.U_2$

Renaming

- $(\rho_\beta(R))(t) = R(t \circ \beta)$
 - $\beta : U \rightarrow U'$ attribute renaming

Evaluation Example

Example

- Semiring is \mathbb{N}
- $q = \sigma_{a=1}(\pi_a(R))$
- $q(t) = \sum_{t'.a=t} R(t') \times (a = 1)(t)$

R

	a	b
2	1	3
3	1	4
2	2	4

	Q	
	a	
$(2 + 3) \times 1 = 5$	1	
$2 \times 0 = 0$	2	

Equivalence Examples

- Union:

- Associative: $R \cup (S \cup T) = (R \cup S) \cup T$
- Commutative: $R \cup S = S \cup R$
- Identity \emptyset : $R \cup \emptyset = R$

- Join

- Associative: $R \bowtie (S \bowtie T) = (R \bowtie S) \bowtie T$
- Commutative: $R \bowtie S = S \bowtie R$

- Selection

- $\sigma_{\text{false}}(R) = \emptyset$
- $\sigma_{\text{true}}(R) = R$

Homomorphisms in Query Evaluation

Homomorphisms commute with Query Evaluation

- $Q(h(I)) = h(Q(I))$
- \Rightarrow We can apply h either before or after evaluating the query without affecting the result

Example

- Homomorphism from \mathbb{N} (bag-semantics) to \mathbb{B} (set-semantics):
 $h(n) = \text{true}$ except $h(0) = \text{false}$
- E.g., $\sigma_{a>1}(R)$

R	
3	1
2	2

R	
<i>true</i>	1
<i>true</i>	2

Provenance Polynomials

Rationale

- Use semiring annotations to model provenance
- Annotate a query result tuple with the semiring expression that was used to compute it
- \Rightarrow need free semiring

Provenance Polynomials Semiring

- $(\mathbb{N}[I], +, \times, 0, 1)$
- $\mathbb{N}[I]$ - Polynomials with natural number exponents
 - Variables: One per tuple in I
- Convention: annotate each instance tuple with a variable named after its tuple id

Provenance Polynomials Example

Example

$$q = \pi_a(R)$$

	R			Q
	a	b		a
t_1	1	2	$t_1 + t_2$	1
t_2	1	3		

Provenance Polynomials Example II

Example

$$q = \pi_{Name}(E \bowtie \sigma_{Dep=CS}(P) \bowtie A)$$

Employee

	Id	Name
e_1	1	Peter
e_2	2	Gertrud
e_2	3	Michael

Assigned

	PName	Id
a_1	Server	1
a_2	Server	2
a_3	Webpage	2
a_4	Fire CS	3

Project

	PName	Dep
p_1	Server	CS
p_2	Webpage	CS
p_3	Fire CS	HR

Provenance Polynomials Example II

Example

$$q = \pi_{Name}(E \bowtie \sigma_{Dep=CS}(P) \bowtie A)$$

$$(q)(t) = \sum_{u.A=t} E(u.E) \times P(u.P) \times (Dep = CS)(u.P) \times A(u.P)$$

Q

$$e_1 \times a_1 \times p_1$$

$$(e_2 \times a_2 \times p_1) + (e_2 \times a_3 \times p_2)$$

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The Fundamental Property

- The semiring of provenance polynomials is the free commutative semiring
- \Rightarrow there exists a homomorphism from $\mathbb{N}[I]$ into any commutative semiring
- $Eval_K : \mathbb{N}[I] \rightarrow K$ is this unique homomorphism defined as
 - Replace each tuple variable t with the element of K assigned to the tuple represented by t
 - Interpret the abstract operations from $\mathbb{N}[I]$ as operations from K

Example Application of the Fundamental Property

Example

$$q = \pi_a(R)$$

		R	
		a	b
t_1		1	2
t_2		1	3

		Q
		a
$t_1 + t_2$		1

Example Application of the Fundamental Property

Example

$$q = \pi_a(R)$$

Interpretation in \mathbb{N}

R		
	a	b
2	1	2
1	1	3

Q
a
$t_1 + t_2$
1

Example Application of the Fundamental Property

Example

$$q = \pi_a(R)$$

Interpretation in \mathbb{N}

		R	
		a	b
2		1	2
1		1	3

$$2 + 1 = 3$$

Q
a
1

The “How” Part

Interpretation of $+$ and \times

- $+$: Alternative use of tuples
 - Operators: Union, Projection
 - Check set-semantics: only one tuples is need $\Rightarrow \vee$ as $+$ operation
 - Check bag-semantics: multiplicities are additive \Rightarrow natural number addition as $+$
- \times : Conjunctive use of tuples
 - Operations: Join
 - Check set-semantics: both tuples are needed $\Rightarrow \wedge$ as \times operation
 - Check bag-semantics: multiplicities of matching tuples are multiplied \Rightarrow natural number multiplication as \times

Insensitivity to Query Rewrite

Bag-semantics

- Modelling relational algebra as commutative semiring operations
 - Possible, because same equivalences
- $\mathbb{N}[I]$ is free commutative semiring
- \Rightarrow Equivalences for $\mathbb{N}[I]$ and bag-semantics are the same!
- $\Rightarrow \mathbb{N}[I]$ is insensitive

Insensitivity to Query Rewrite

Set-semantics

- $\mathbb{N}[I]$ no longer insensitive
 - E.g., $R \neq R \bowtie R$
- $\mathbb{B}[I]$: polynomials with boolean coefficients and exponents has same equivalences as set semantics
- There exists an homomorphism from $\mathbb{N}[I]$ to $\mathbb{B}[I]$ ($\mathbb{N}[I]$ is free object!)
- \Rightarrow apply equivalences of $\mathbb{B}[I]$ to $\mathbb{N}[I]$ then insensitive for set-semantics

How-provenance

Notation

- We write $\mathbb{N}[I](q, t)$ for
- $(q)(t)$ evaluated in $\mathbb{N}[I]$
- also use this for other semirings K

Beyond Positive Relational Algebra

Set Difference

- Need additional operator –
- \Rightarrow from semiring to structures $(S, +, \times, -, 1, 0)$
 - Different equivalences hold!
- Provenance use (more complex) free object for such structures

Aggregation

- Annotate attribute values with combinations of
 - tuple semiring provenance
 - annotation for values for computations on values (representing aggregation)

Outline

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 - Introduction
 - Semiring Semantics for Relational Algebra
 - How-Provenance or Provenance Polynomials
 - Relationship to other Provenance Models
 - ORCHESTRA
 - Recap

Relationship of Provenance Polynomials and other Provenance Models

Rationale

- How is the provenance polynomials model related to other provenance models?
- Can we find semirings that models, e.g., Why-Provenance?

Why-Provenance

Semiring

- $K_{Why} = (\mathcal{P}(\mathcal{P}(I)), \cup, \uplus, \emptyset, \{\emptyset\})$
- \mathcal{P} = powerset
- $\Rightarrow \mathcal{P}(\mathcal{P}(I))$ is all sets containing subsets of the instance I
- \Rightarrow all potential sets of witnesses
- $+$ is normal set union
- \times is $S_1 \uplus S_2 = \{(a \cup b) \mid a \in S_1 \wedge b \in S_2\}$
 - \Rightarrow pairwise union
 - \Rightarrow combining witnesses

Why-Provenance

Example

$$q = \pi_{Name}(E \bowtie \sigma_{Dep=CS}(P) \bowtie A)$$

$$(q)(t) = \sum_{u.A=t} E(u.E) \times P(u.P) \times (Dep = CS)(u.P) \times A(u.P)$$

Q

 $\{\{e_1, a_1, p_1\}\}$ $\{\{e_2, a_2, p_1\}, \{e_2, a_3, p_2\}\}$

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BY

Insensitive Why-Provenance

Semiring

- $K_{IWhy} = (min(\mathcal{P}(\mathcal{P}(I))), \cup_{min}, \uplus_{min}, \emptyset, \{\emptyset\})$
- $\Rightarrow \mathcal{P}(\mathcal{P}(I))$ is all sets containing subsets of the instance I
- $min(S) = \{a \mid a \in S \wedge \nexists b \in S : b \subseteq a\}$
- $S_1 \cup_{min} S_2 = min(S_1 \cup S_2)$
- $S_1 \uplus_{min} S_2 = min(S_1 \uplus S_2)$
- \Rightarrow Same operations, compute minimal elements

Insensitive Why-Provenance

Example

$$q = \pi_{Name}(E \bowtie \sigma_{Dep=CS}(P) \bowtie A)$$

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Insensitive Why-Provenance

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Insensitive Why-Provenance

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Fire CS	HR

BY

Lineage

Different Model

- The inventors of provenance polynomials consider a slightly different Lineage model
- Provenance is a **set of tuples** instead of a **list of sets of tuples**

Semiring

- $K_{Lin} = (\mathcal{P}(I), \cup_{\perp}, \cup_{\perp}^*, \perp, \emptyset)$
- $\Rightarrow \mathcal{P}(I)$ is all subsets of the instance I
- \perp is a not defined element
- \cup_{\perp} and \cup_{\perp}^* are union with different behaviour on \perp
- $\perp \cup_{\perp} S = S \cup_{\perp} \perp = S$
- $\perp \cup_{\perp}^* S = S \cup_{\perp}^* \perp = \emptyset$

Lineage

Example

$$q = \pi_{Name}(E \bowtie \sigma_{Dep=CS}(P) \bowtie A)$$

$$(q)(t) = \sum_{u.A=t} E(u.E) \times P(u.P) \times (Dep = CS)(u.P) \times A(u.P)$$

Q

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 $\{e_1, a_1, p_1\}$ $\{e_2, a_2, a_3, p_1, p_2\}$

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Lineage

“Real” Lineage

- Can we also model the **list of sets of tuples** lineage as a semiring?

Lineage

“Real” Lineage

- Can we also model the **list of sets of tuples** lineage as a semiring?
- **NO!**:
 - Assume existence of semiring K_{RLin} that models lineage
 - Equivalent queries $q = R \cup S$ and $q' = S \cup R$
 - Assume tuple t is in the result of q/q' and was derived from r_1 and s_1
 - Lineage: $Lin(q, t) = \langle \{r_1\}, \{s_1\} \rangle \neq \langle \{s_1\}, \{r_1\} \rangle = Lin(q', t)$
 - Evaluation in K_{RLin} : $(q)(t) = r_1 + s_1 = s_1 + r_1 = (q')(t)$
 - \Rightarrow no assumptions except that K_{RLin} is semiring
 - $\Rightarrow K_{RLin}$ cannot exist

Perm Influence Contribution Semantics

Semiring

- Cannot exist for the same reason as Lineage
 - Assume existence of semiring K_{PI} that models PI-CS
 - Equivalent queries $q = R \cup S$ and $q' = S \cup R$
 - Assume tuple t is in the result of q/q' and was derived from r_1 and s_1
 - Lineage: $PI(q, t) = \{ \langle r_1, s_1 \rangle \} \neq \{ \langle s_1, r_1 \rangle \} = PI(q', t)$
 - Evaluation in K_{PI} : $(q)(t) = r_1 + s_1 = s_1 + r_1 = (q')(t)$
 - $\Rightarrow K_{PI}$ cannot exist

Perm Influence Contribution Semantics

Discussion

- Lineage and PI-CS consider the order of leaves in the algebra tree
- However, equivalent queries can have different orders
- If we abstract from the order, is the result expressible in the semiring model?
- **Rationale:** Define mapping H from \mathcal{PI} to $\mathbb{N}[I]$ that gets rid of the order

Perm Influence Contribution Semantics

From \mathcal{PI} to $\mathbb{N}[I]$

- Witness-lists are basically \times
- The set of witness-lists is basically $+$

$$H(\mathcal{PI}(q, t)) = \sum_{w \in \mathcal{PI}(q, t)} \prod_{i \in \{1, \dots, n\}} w'[i]$$

$$w'[i] = \begin{cases} w[i] & \text{if } w[i] \neq \perp \\ 1 & \text{otherwise} \end{cases}$$

Perm Influence Contribution Semantics

Example

$$q = \pi_a(R) \cup (\pi_a(R \bowtie S))$$

$$PI(q, t_1) = \{ \langle r_1, \perp \rangle, \langle r_1, s_1 \rangle \}$$

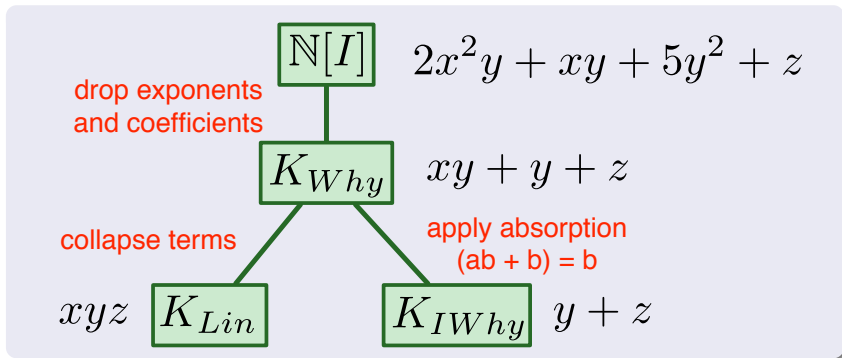
$$\begin{aligned} H(PI(q, t_1)) &= \sum_{w \in PI(q, t_1)} \prod_{i \in \{1, \dots, n\}} w'[i] \\ &= r_1 \times 1 + r_1 \times s_1 = r_1 + r_1 \times s_1 \\ &= \mathbb{N}[I](q, t_1) \end{aligned}$$

	S
	b
r_1	1
r_2	2

	S
	a
s_1	1

	Q
	a
t_1	1
t_2	2

Relationships between Provenance Semirings



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ORCHESTRA

Overview

- Collaborative **D**ata **S**haring **S**ystem
- Network of peers
- Each peer has independent schema and instance
- Peers update their instances without restrictions
- Schema mappings define relationships between schemata
 - Can be partial
- Periodically peers trigger exchange of updates based on mappings

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Recap

Semiring Semantics for the Relational Model

- Alternative semantics for relational algebra
- Given a semiring $(K, +, \times, 0, 1)$
 - K -relations are functions from tuples of an arity U to semiring elements
 - Operators take functions (relations) as input and produce an output function (relation)
- Using different semirings we get standard semantics or extensions of the relational model
 - $(\mathbb{B}, \vee, \wedge, \text{false}, \text{true})$: Set semantics
 - $(\mathbb{N}, +, \times, 0, 1)$: Bag semantics
 - $(\text{PosBool}(X), \vee, \wedge, \text{false}, \text{true})$: c -tables

Recap

How-Provenance (Provenance semiring)

- **Rationale:** Provenance for t is expression that represent the semiring computation that lead to creation of tuple t .
- **Representation:** Polynomial over tuple variables (= **element of Provenance Semiring**)
- **Syntactic Definition:**
 - For USPJ queries + extensions for A and D
- **The Fundamental Property:** Given an query result in $\mathbb{N}[I]$, we can compute the query result for any semiring K from that
- **Relation to other Provenance Types:**
 - Semirings that model other provenance models
 - Why-Provenance: $(\mathcal{P}(\mathcal{P}(I)), \cup, \uplus, \emptyset, \{\emptyset\})$
 - IWhy-Provenance: $(\min(\mathcal{P}(I)), \cup_{min}, \times_{min}, \emptyset, \{\emptyset\})$
 - Lineage*: $(\mathcal{P}(I) \cup \{\perp\}, +, \times, \perp, \emptyset)$

Recap

ORCHESTRA

- Peer-to-Peer update exchange system
- Schema mappings between peers
- Updates are exchanged between periodically based on mappings
- Provenance used for
 - Trust
 - Deletion propagation

Literature II



F. Geerts and A. Poggi.

On database query languages for K-relations.
Journal of Applied Logic, 8(2):173–185, 2010.



Todd J. Green.

Containment of Conjunctive Queries on Annotated Relations.
In ICDT '09: Proceedings of the 16th International Conference on Database Theory, 296–309, 2009.



Todd J. Green.

Collaborative data sharing with mappings and provenance.
PhD thesis, University of Pennsylvania, 2009.



Todd J. Green, Zachary G. Ives, and Val Tannen.

Reconcilable differences.
In ICDT '09: Proceedings of the 16th International Conference on Database Theory, 212–224, Saint Petersburg, Russia, March 2009. , .



Zachary G. Ives, Todd J. Green, Grigoris Karvounarakis, Nicholas E. Taylor, Val Tannen, Partha Pratim Talukdar, Marie Jacob, and Fernando Pereira.
The ORCHESTRA Collaborative Data Sharing System.
SIGMOD Record, 37(2):26–32, 2008.



J. Nathan Foster, Todd J. Green, and Val Tannen.

Annotated XML: Queries and Provenance.
In PODS '08: Proceedings of the 27th Symposium on Principles of Database Systems, 2008.

Literature III



Todd J. Green, Gregory Karvounarakis, and Val Tannen.

Provenance Semirings.

In PODS '07: Proceedings of the 26th Symposium on Principles of Database Systems, 31–40, 2007.



Todd J. Green, Grigoris Karvounarakis, Nicholas E. Taylor, Olivier Biton, Zachary G. Ives, and Val Tannen.

ORCHESTRA: Facilitating Collaborative Data Sharing.

In SIGMOD '07: Proceedings of the 33th SIGMOD International Conference on Management of Data, 2007.



Todd J. Green, Grigoris Karvounarakis, Zachary G. Ives, and Val Tannen.

Update Exchange with Mappings and Provenance.

In VLDB '07: Proceedings of the 33th International Conference on Very Large Data Bases, 675–686, 2007.



Floris Geerts and Jan Van den Bussche.

Relational Completeness of Query Languages for Annotated Databases.

Lecture Notes in Computer Science, 4797:127, 2007.



Zachary G. Ives, Nitin Khandelwal, Aneesh Kapur, and Murat Cakir.

ORCHESTRA: Rapid, Collaborative Sharing of Dynamic Data.

In CIDR '05: Proceedings of the 2th Conference on Innovative Data Systems Research, 2005.