

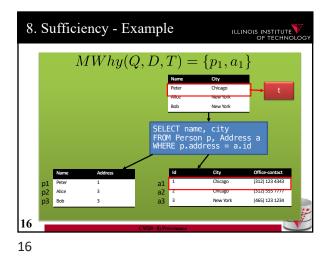
8. Minimality
Rationale:

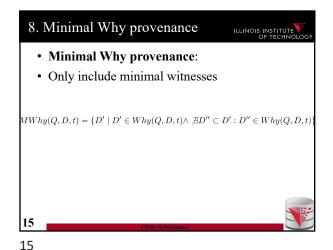
Remove tuples that do not contribute to the result
If a subset of a witness is already sufficient then everything not in the subset is unnecessary and should be removed

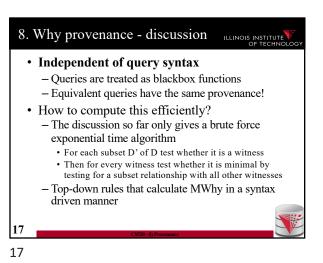
Definition

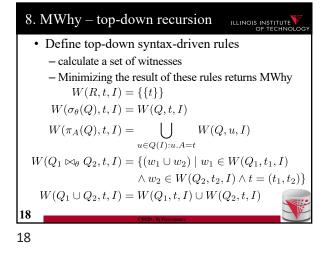
witness D' is minimal if ∀D'' ⊂ D' : Q(D'') ≠ Q(D)

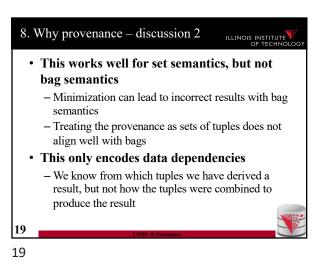
14 (COLP. PROMACE)

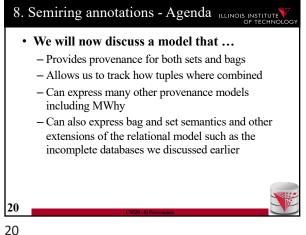


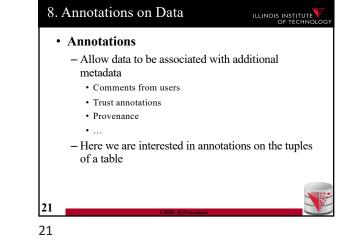


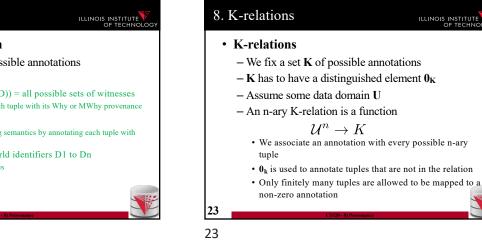












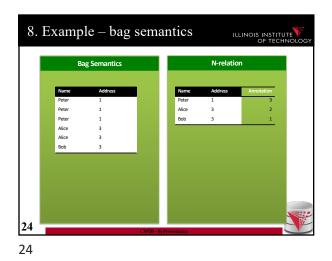




- Annotation domain
 - We fix a set K of possible annotations
 - Examples

• Powerset(Powerset(D)) = all possible sets of witnesses - We can annotate each tuple with its Why or MWhy provenance Natural numbers

- We can simulate bag semantics by annotating each tuple with its multiplicity
- A set of possible world identifiers D1 to Dn - Incomplete databases



8. Example – incomplete DBs

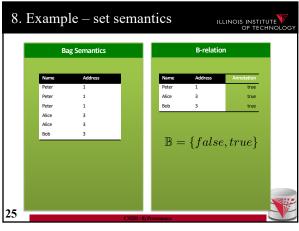
Incomplet Database

 D_1

2

 D_2

2



25

{D1}

{D2}

{D1,D2}

-relation

2

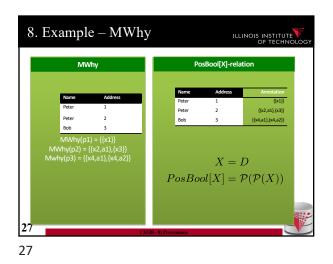
2

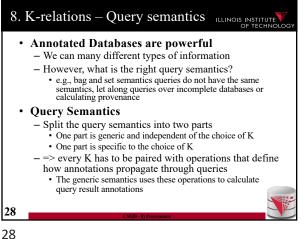
 $= \{\emptyset, \{D_1\}, \{D_2\}, \{D_1, D_2\}\}$

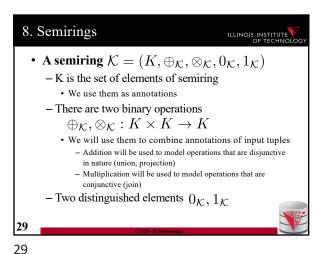
Peter

Alice

 $\Omega = \mathcal{P}(\{D_1, D_2\})$

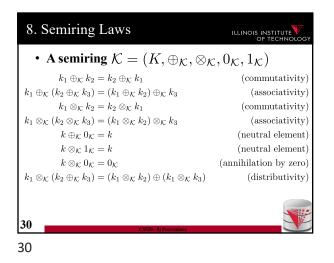


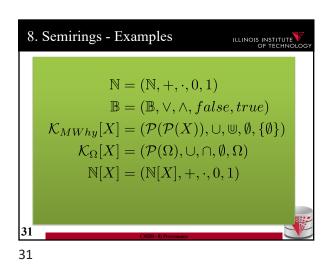


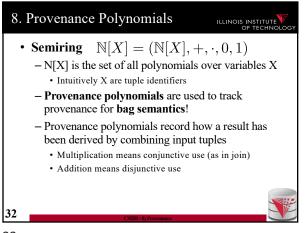


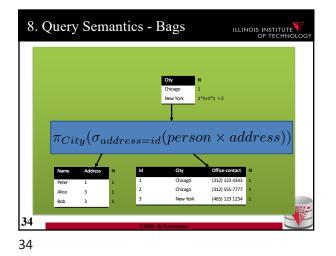
26

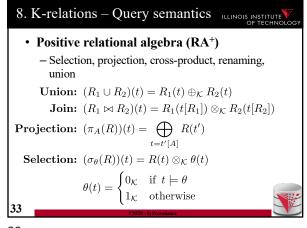
26



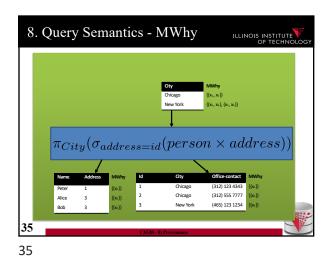


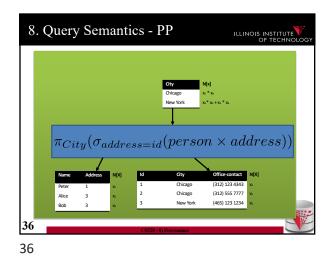


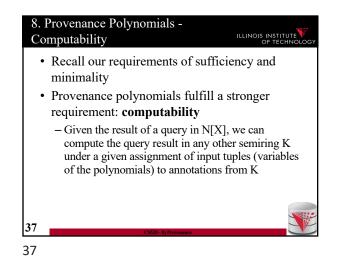


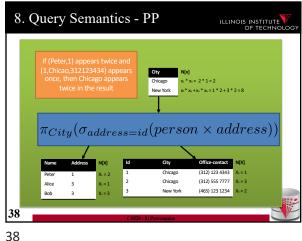














8. Fundamental theorem



• Theorem: Homomorphism commute with queries O(I(D))

$$Q(h(D)) = h(Q(D))$$

- Proof Sketch: queries are defined using semiring operations which commute with homomorphisms
- Theorem: Any assignment X -> K induces a semiring homomorphism $N[X] \rightarrow K$
- 40 40

