# CS425 - Summer 2016 Jason Arnold Chapter 7: Entity-Relationship Model 

Partially taken from
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## Requirement Analysis Example Zoo

n The zoo stores information about animals, cages, and zoo keepers.
$n \quad$ Animals are of a certain species and have a name. For each animal we want to record its weight and age.
$n$ Each cage is located in a section of the zoo. Cages can house animals, but there may be cages that are currently empty. Cages have a size in square meter.
$n \quad$ Zoo keepers are identified by their social security number. We store a first name, last name, and for each zoo keeper. Zoo keepers are assigned to cages they have to take care of (clean, ...). Each cage that is not empty has a zoo keeper assigned to it. A zoo keeper can take care of several cages. Each zoo keeper takes care of at least one cage.

## Modeling - ER model

n A database can be modeled as:
। a collection of entities,
। relationship among entities.
$n \quad$ An entity is an object that exists and is distinguishable from other objects.
। Example: specific person, company, event, plant
n Entities have attributes
I Example: people have names and addresses
$n \quad$ An entity set is a set of entities of the same type that share the same properties.
| Example: set of all persons, companies, trees, holidays

## Entity Sets instructor and student



## Relationship Sets

$n$ A relationship is an association among several entities Example:

| 44553 (Peltier) | $\underline{\text { advisor }}$ |
| :--- | :---: | :---: |
| student entity |  |$\quad$| 22222 (Elationship set (Ein) |
| :---: |
| instructor entity |

$n$ A relationship set is a mathematical relation among $n \geq 2$ entities, each taken from entity sets

$$
\left\{\left(e_{1}, e_{2}, \ldots e_{n}\right) \mid e_{1} \in E_{1}, e_{2} \in E_{2}, \ldots, e_{n} \in E_{n}\right\}
$$

where $\left(e_{1}, e_{2}, \ldots, e_{n}\right)$ is a relationship
। Example:
$(44553,22222) \in$ advisor

## Relationship Set advisor

| 76766 | Crick | 98988 | Tanaka |
| :---: | :---: | :---: | :---: |
| 45565 | Katz | 12345 | Shankar |
| 10101 | Srinivasan | 00128 | Zhang |
| 98345 | Kim | 76543 | Brown |
| 76543 | Singh | 76653 | Aoi |
| 22222 | Einstein | 23121 | Chavez |
|  | structor | 44553 | Peltier |

## Relationship Sets (Cont.)

n An attribute can also be property of a relationship set.
n For instance, the advisor relationship set between entity sets instructor and student may have the attribute date which tracks when the student started being associated with the advisor

| 76766 | Crick | Tanaka |
| :---: | :---: | :---: |
| 45565 | Katz | Shankar |
| 10101 | Srinivasan | Zhang |
| 98345 | Kim | Brown |
| 76543 | Singh | Aoi |
| 22222 | Einstein | Chavez |
|  | tructor | Peltier |

## Degree of a Relationship Set

n binary relationship
। involve two entity sets (or degree two).
n Relationships between more than two entity sets are rare. Most relationships are binary. (More on this later.)

- Example: students work on research projects under the guidance of an instructor.
- relationship proj_guide is a ternary relationship between instructor, student, and project


## Attributes

n An entity is represented by a set of attributes, that are descriptive properties possessed by all members of an entity set.
। Example:

$$
\begin{aligned}
& \text { instructor = (ID, name, street, city, salary }) \\
& \text { course= (course_id, title, credits) }
\end{aligned}
$$

$n$ Domain - the set of permitted values for each attribute
n Attribute types:
| Simple and composite attributes.
। Single-valued and multivalued attributes
, Example: multivalued attribute: phone_numbers
। Derived attributes

- Can be computed from other attributes
- Example: age, given date_of_birth


## Composite Attributes



## Mapping Cardinality Constraints

$n$ Express the number of entities to which another entity can be associated via a relationship set.
n For a binary relationship set the mapping cardinality must be one of the following types:
। One to one (1-1)
। One to many (1-N)
। Many to one ( $\mathrm{N}-1$ )
। Many to many (N-M)

## Mapping Cardinalities



Note: Some elements in $A$ and $B$ may not be mapped to any elements in the other set

## Mapping Cardinalities Example



Note: Some elements in $A$ and $B$ may not be mapped to any elements in the other set

## Mapping Cardinalities Example



Note: Some elements in A and B may not be mapped to any elements in the other set

## Mapping Cardinality Constraints Cont.

n What if we allow some elements to not be mapped to another element?
| E.g., 0:1-1
n For a binary relationship set the mapping cardinality must be one of the following types:

| n | 1-1 |
| :---: | :---: |
|  | \| 1-1 |
|  | \| 0:1-1 |
|  | 1-0:1 |
|  | \| 0:1-0:1 |
| n | 1-N |
|  | - 0:1-N |
|  | \| 0:1-0:N |
|  | - 1-N |
|  | \| 1-0:N |

n N -1
I N-1
| N-0:1
| 0:N-1
| 0:N-0:1
n $\mathbf{N}-\mathrm{M}$
I N-M
I N-0:M
I O:N-M
| O:N-O:M

## Mapping Cardinality Constraints Cont.

n Typical Notation<br>$(0: 1)-(1: N)$

## Keys

n A super key of an entity set is a set of one or more attributes whose values uniquely determine each entity.
$n \quad$ A candidate key of an entity set is a minimal super key
। ID is candidate key of instructor
I course_id is candidate key of course
n Although several candidate keys may exist, one of the candidate keys is selected to be the primary key.
n Note: Basically the same as for relational model

## Keys for Relationship Sets

$n$ The combination of primary keys of the participating entity sets forms a super key of a relationship set.
। (s_id, i_id) is the super key of advisor
NOTE: this means a pair of entities can have at most one relationship in a particular relationship set.

- Example: if we wish to track multiple meeting dates between a student and her advisor, we cannot assume a relationship for each meeting. We can use a multivalued attribute though or model meeting as a separate entity
n Must consider the mapping cardinality of the relationship set when deciding what are the candidate keys
$\mathrm{n} \quad$ Need to consider semantics of relationship set in selecting the primary key in case of more than one candidate key


## Keys for Relationship Sets Cont.

n Must consider the mapping cardinality of the relationship set when deciding what are the candidate keys

1-1: both primary keys are candidate keys
, Example: hasBc: (Person-Birthcertificate)
। N -1: the N side is the candidate key

- Example: worksFor: (Instructor-Department)

I N-M: the combination of both primary keys
, Example: takes: (Student-Course)

## Redundant Attributes

n Suppose we have entity sets
। instructor, with attributes including dept_name
। department
and a relationship
। inst_dept relating instructor and department
n Attribute dept_name in entity instructor is redundant since there is an explicit relationship inst_dept which relates instructors to departments

The attribute replicates information present in the relationship, and should be removed from instructor

। BUT: when converting back to tables, in some cases the attribute gets reintroduced, as we will see.

## E-R Diagrams


n Rectangles represent entity sets.
n Diamonds represent relationship sets.
n Attributes listed inside entity rectangle
n Underline indicates primary key attributes

## Entity With Composite, Multivalued, and Derived Attributes

| instructor |
| :---: |
| $\underline{\text { ID }}$ |
| name |
| first_name |
| middle_initial |
| last_name |
| address |
| street |
| street_number |
| street_name |
| apt_number |
| city |
| state |
| zip |
| \{phone_number \} |
| date_of_birth |
| age ( ) |

## Entity With Composite, Multivalued, and Derived Attributes



## Relationship Sets with Attributes



## Roles

n Entity sets of a relationship need not be distinct
। Each occurrence of an entity set plays a "role" in the relationship
n The labels "course_id" and "prereq_id" are called roles.


## Cardinality Constraints

n We express cardinality constraints by drawing either a directed line $(\rightarrow)$, signifying "one," or an undirected line (-), signifying "many," between the relationship set and the entity set.
n One-to-one relationship:
I A student is associated with at most one instructor via the relationship advisor
। A student is associated with at most one department via stud_dept

## One-to-One Relationship

n one-to-one relationship between an instructor and a student
। an instructor is associated with at most one student via advisor
I and a student is associated with at most one instructor via advisor


## One-to-Many Relationship

n one-to-many relationship between an instructor and a student
I an instructor is associated with several (including 0) students via advisor

I a student is associated with at most one instructor via advisor,

| instructor |
| :--- | :--- |
| ID <br> name <br> salary |

## Many-to-One Relationships

n In a many-to-one relationship between an instructor and a student,
। an instructor is associated with at most one student via advisor,

I and a student is associated with several (including 0) instructors via advisor


## Many-to-Many Relationship

n An instructor is associated with several (possibly 0 ) students via advisor
$n$ A student is associated with several (possibly 0 ) instructors via advisor


## Participation of an Entity Set in a Relationship Set

$n \quad$ Total participation (indicated by double line): every entity in the entity set participates in at least one relationship in the relationship set
| E.g., participation of section in sec_course is total

- every section must have an associated course
n Partial participation: some entities may not participate in any relationship in the relationship set

। Example: participation of instructor in advisor is partial


## Alternative Notation for Cardinality Limits

n Cardinality limits can also express participation constraints

| instructor |  | student |  |
| :--- | :--- | :--- | :--- |
| $\underline{I D}$ <br> name <br> salary | $0 . . *$ | advisor | ID <br> name <br> tot_cred |

## Alternative Notation for Cardinality Limits

n Alternative Notation

| instructor |  | 1.1 | student |
| :---: | :---: | :---: | :---: |
| ID |  |  | ID |
| name salary | (0,n) | $(1,1)$ | name tot cred |

## E-R Diagram with a Ternary Relationship



## Cardinality Constraints on Ternary Relationship

n We allow at most one arrow out of a ternary (or greater degree) relationship to indicate a cardinality constraint
$n$ E.g., an arrow from proj_guide to instructor indicates each student has at most one guide for a project
$n$ If there is more than one arrow, there are two ways of defining the meaning.
। E.g., a ternary relationship $R$ between $A, B$ and $C$ with arrows to $B$ and $C$ could mean

1. each $A$ entity is associated with a unique entity from $B$ and $C$ or
2. each pair of entities from $(A, B)$ is associated with a unique $C$ entity, and each pair $(A, C)$ is associated with a unique $B$

। Each alternative has been used in different formalisms
। To avoid confusion we outlaw more than one arrow
n Better to use cardinality constraints such as $(0, n)$

## Weak Entity Sets

n An entity set that does not have a primary key is referred to as a weak entity set.
$n$ The existence of a weak entity set depends on the existence of a identifying entity set
। It must relate to the identifying entity set via a total, one-to-many relationship set from the identifying to the weak entity set
। Identifying relationship depicted using a double diamond
n The discriminator (or partial key) of a weak entity set is the set of attributes that distinguishes among all the entities of a weak entity set that are associated with the same entity of the identifying entity set
n The primary key of a weak entity set is formed by the primary key of the strong entity set on which the weak entity set is existence dependent, plus the weak entity set's discriminator.

## Weak Entity Sets (Cont.)

n We underline the discriminator of a weak entity set with a dashed line.
n We put the identifying relationship of a weak entity in a double diamond.
n Primary key for section - (course_id, sec_id, semester, year)


## Weak Entity Sets (Cont.)

$n$ Note: the primary key of the strong entity set is not explicitly stored with the weak entity set, since it is implicit in the identifying relationship.
$n$ If course_id were explicitly stored, section could be made a strong entity, but then the relationship between section and course would be duplicated by an implicit relationship defined by the attribute course_id common to course and section

## E-R Diagram for a University Enterprise



## Reduction to Relational Schemas

## Representing Entity Sets With Simple Attributes

n A strong entity set reduces to a schema with the same attributes student(ID, name, tot_cred)
n A weak entity set becomes a table that includes a column for the primary key of the identifying strong entity set section (course id, sec id, sem, year )


## Representing Relationship Sets

n A many-to-many relationship set is represented as a schema with attributes for the primary keys of the two participating entity sets, and any descriptive attributes of the relationship set.
n Example: schema for relationship set advisor
advisor $=(\underline{s i d}, i \quad i d)$


## Redundancy of Schemas

n Many-to-one and one-to-many relationship sets that are total on the many-side can be represented by adding an extra attribute to the "many" side, containing the primary key of the "one" side
n Example: Instead of creating a schema for relationship set inst_dept, add an attribute dept_name to the schema arising from entity set instructor


## Redundancy of Schemas (Cont.)

n For one-to-one relationship sets, either side can be chosen to act as the "many" side
। That is, extra attribute can be added to either of the tables corresponding to the two entity sets
I If the relationship is total in both sides, the relation schemas from the two sides can be merged into one schema
$n$ If participation is partial on the "many" side, replacing a schema by an extra attribute in the schema corresponding to the "many" side could result in null values
$n \quad$ The schema corresponding to a relationship set linking a weak entity set to its identifying strong entity set is redundant.
I Example: The section schema already contains the attributes that would appear in the sec_course schema

## Composite and Multivalued Attributes

## instructor

## ID

name
first_name middle_initial
last_name
address
street
street_number
street_name
apt_number
city
state
zip
\{ phone_number \}
date_of_birth age ()
n Composite attributes are flattened out by creating a separate attribute for each component attribute
| Example: given entity set instructor with composite attribute name with component attributes first_name and last_name the schema corresponding to the entity set has two attributes name_first_name and name_last_name

- Prefix omitted if there is no ambiguity
n Ignoring multivalued attributes, extended instructor schema is
। instructor(ID,
first_name, middle_initial, last_name, street_number, street_name,
apt_number, city, state, zip_code, date_of_birth)


## Composite and Multivalued Attributes

n A multivalued attribute $M$ of an entity $E$ is represented by a separate schema EM
। Schema $E M$ has attributes corresponding to the primary key of $E$ and an attribute corresponding to multivalued attribute $M$
। Example: Multivalued attribute phone_number of instructor is represented by a schema:
inst_phone $=(\underline{I D}$, phone number $)$
। Each value of the multivalued attribute maps to a separate tuple of the relation on schema EM

- For example, an instructor entity with primary key 22222 and phone numbers 456-7890 and 123-4567 maps to two tuples:
(22222, 456-7890) and (22222, 123-4567)


## Multivalued Attributes (Cont.)

n Special case:entity time_slot has only one attribute other than the primary-key attribute, and that attribute is multivalued
। Optimization: Don' t create the relation corresponding to the entity, just create the one corresponding to the multivalued attribute
। time_slot(time_slot_id, day, start_time, end_time)
| Caveat: time_slot attribute of section (from sec_time_slot) cannot be a foreign key due to this optimization


## Design Issues

n Use of entity sets vs. attributes

| instructor |
| :--- |
| $\frac{I D}{\text { name }}$ |
| salary |
| phone_number |


n Designing phone as an entity allow for primary key constraints for phone
$n$ Designing phone as an entity allow phone numbers to be used in relationships with other entities (e.g., student)
$n$ Use of phone as an entity allows extra information about phone numbers

## Design Issues

n Use of entity sets vs. relationship sets
। Possible guideline is to designate a relationship set to describe an action that occurs between entities
। Possible hint: the relationship only relates entities, but does not have an existence by itself. E.g., hasAddress: (department-address)


## Design Issues

n Binary versus n -ary relationship sets
Although it is possible to replace any nonbinary ( $n$-ary, for $n>2$ ) relationship set by a number of distinct binary relationship sets + an aritifical entity set, a $n$-ary relationship set shows more clearly that several entities participate in a single relationship.

## Binary Vs. Non-Binary Relationships

n Some relationships that appear to be non-binary may be better represented using binary relationships
E.g., A ternary relationship parents, relating a child to his/her father and mother, is best replaced by two binary relationships, father and mother

I But there are some relationships that are naturally non-binary

- Example: proj_guide


## Converting Non-Binary Relationships to Binary Form

n In general, any non-binary relationship can be represented using binary relationships by creating an artificial entity set.

Replace $R$ between entity sets $A, B$ and $C$ by an entity set $E$, and three relationship sets:

1. $R_{A}$, relating $E$ and $A \quad$ 2. $R_{B}$, relating $E$ and $B$
2. $R_{C}$, relating $E$ and $C$

। Create a special identifying attribute for $E$
। Add any attributes of $R$ to $E$
I For each relationship $\left(a_{i}, b_{i}, c_{i}\right)$ in $R$, create

1. a new entity $e_{i}$ in the entity set $E$
2. add $\left(e_{i}, a_{i}\right)$ to $R_{A}$
3. add ( $e_{i}, b_{i}$ ) to $R_{B}$
4. add $\left(e_{i}, c_{i}\right)$ to $R_{C}$

(b)

## ER-model to Relational Summary

n Rule 1) Strong entity E
। Create relation with attributes of $E$
। Primary key is equal to the PK of $E$
n Rule 2) Weak entity W identified by E through relationship $R$
। Create relation with attributes of $W$ and $R$ and $P K(E)$.
Set $P K$ to discriminator attributes combined with $P K(E) . P K(E)$ is a foreign key to $E$.
n Rule 3) Binary relationship $R$ between $A$ and $B$ : one-to-one
If no side is total add PK of $A$ to as foreign key in $B$ or the other way around. Add any attributes of the relationship $R$ to $A$ respective $B$.
। If one side is total add PK of the other-side as foreign key. Add any attributes of the relationship $R$ to the total side.
। If both sides are total merge the two relation into a new relation $E$ and choose either PK(A) as PK(B) as the new PK. Add any attributes of the relationship $R$ to the new relation $E$.

## ER-model to Relational Summary (Cont.)

n Rule 4) Binary relationship $R$ between $A$ and B: one-to-many/many-toone

I Add PK of the "one" side as foreign key to the "many" side.
। Add any attributes of the relationship $R$ to the "many" side.
n Rule 5) Binary relationship $R$ between $A$ and $B$ : many-to-many
। Create a new relation $R$.
। Add PK's of $A$ and $B$ as attributes + plus all attributes of $R$.
I The primary key of the relationship is $P K(A)+P K(B)$. The $P K$ attributes of $A / B$ form a foreign key to $A / B$
$n$ Rule 6) $N$-ary relationship $R$ between $E_{1} \ldots E_{n}$
। Create a new relation.
। Add all the PK's of $E_{1} \ldots E_{n}$. Add all attributes of $R$ to the new relation.

। The primary key or $R$ is $\operatorname{PK}\left(E_{1}\right)$... $\operatorname{PK}\left(E_{n}\right)$. Each $\operatorname{PK}\left(E_{i}\right)$ is a foreign key to the corresponding relation.

## ER-model to Relational Summary (Cont.)

n Rule 7) Entity E with multi-valued attribute A
। Create new relation. Add $A$ and $P K(E)$ as attributes.
। PK is all attributes. $P K(E)$ is a foreign key.

## E-R Diagram for a University Enterprise



## Translate the University ER-Model

n Rule 1) Strong Entities
department(dept name, building, budget)
instructor(ID, name, salary)
। student(ID, name, tot_cred)
। course(course id, title, credits)
| time_slot(time_slot_id)
। classroom(building,room_number, capacity)
n Rule 2) Weak Entities
। section(course id, sec id, semester, year)

## Translate the University ER-Model

n Rule 3) Relationships one-to-one
। None exist
n Rule 4) Relationships one-to-many
। department(dept name, building, budget)
। instructor(ID, name, salary, dept_name)
। student(ID, name, tot_cred, dept_name, instr_ID)


। course(course id, title, credits, dept_name)
| time_slot(time_slot_id)
। classroom(building,room_number, capacity)
I section(course id, sec id, semester, year, room_building, room_number, time_slot_id)

## Translate the University ER-Model

n Rule 5) Relationships many-to-many
department(dept_name, building, budget)
instructor(ID, name, salary, dept_name)
student(ID, name, tot_cred, dept_name, instr_ID)
course(course id, title, credits, dept_name)
time_slot(time_slot_id)
classroom(building,room number, capacity)
section(course id, sec id, semester, year, room_building, room_number, time_slot_id)
prereq(course id, prereq id)
। teaches(ID, course id, sec id, semester, year)
। takes(ID, course id, sec id, semester, year, grade)


## Translate the University ER-Model

n Rule 7) Multivalued attributes
department(dept name, building, budget)
instructor(ID, name, salary, dept_name)
student(ID, name, tot_cred, dept_name, instr_ID)
course(course id, title, credits, dept_name)
time_slot(time_slot_id)
time_slot_day(time_slot id, start time, end time)
classroom(building,room number, capacity)
section(course id, sec id, semester, year, room_building, room_number, time_slot_id)
prereq(course id, prereq_id)
I teaches(ID, course id, sec id, semester, year)
। takes(ID, course id, sec id, semester, year, grade)

## ER Design Decisions

n The use of an attribute or entity set to represent an object.
n Whether a real-world concept is best expressed by an entity set or a relationship set.
n The use of a ternary relationship versus a pair of binary relationships.
$n \quad$ The use of a strong or weak entity set.
n The use of specialization/generalization - contributes to modularity in the design.
$n$ The use of aggregation - can treat the aggregate entity set as a single unit without concern for the details of its internal structure.

## Summary of Symbols Used in E-R Notation

attributes:
simple (A1), composite (A2) and multivalued (A3) derived (A4)
primary key
discriminating attribute of weak entity set

## End of Chapter 7

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